
Basic 12

Micro-nano Thermodynamics

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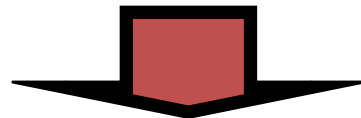
Micro-nano Thermodynamics

Thermodynamics

- Progress limitation of phenomenon (Process)

||

Equilibrium



Evaluation standard of system design

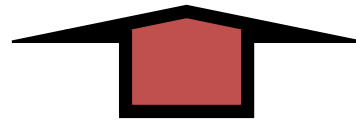
- 1) Thermodynamics for **material**
- 2) Thermodynamics for **process**
- 3) Thermodynamics for **system**



1) Thermodynamics for material

Energy of material: E

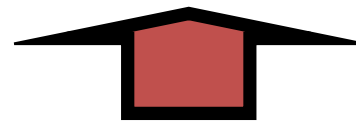
Entropy of material: S



The number of material phases
Concentrations of material in each phase
Temperature
Pressure

Unit of energy: [J], [J/s]

Unit of entropy: [J/K], [J/(K·s)]

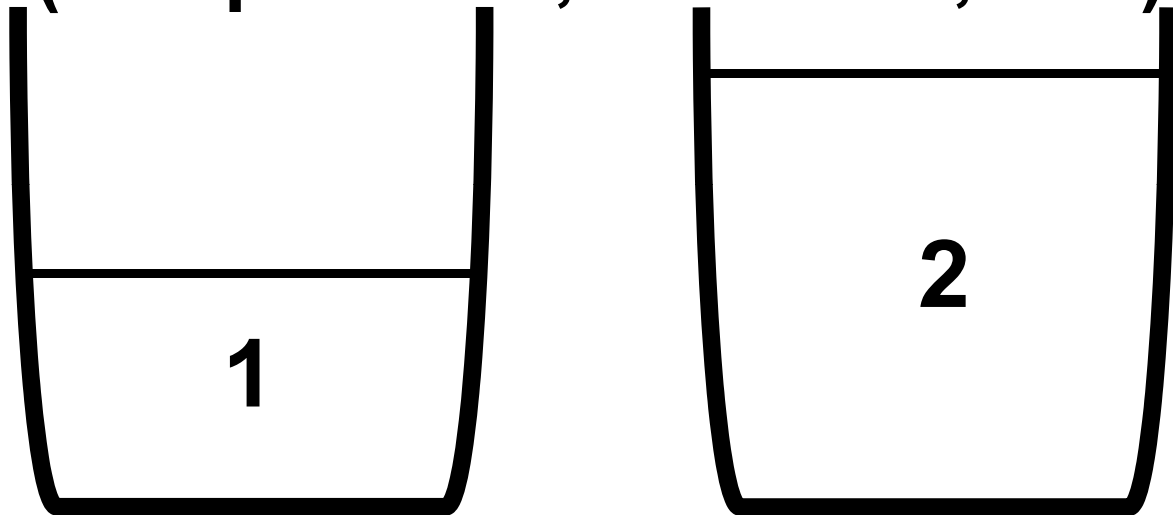


Explanation by Water model



Ex. 1 Water in a flask (Batch)

Same conditions
(Temperature, Pressure, etc.)



Energy

E [J]

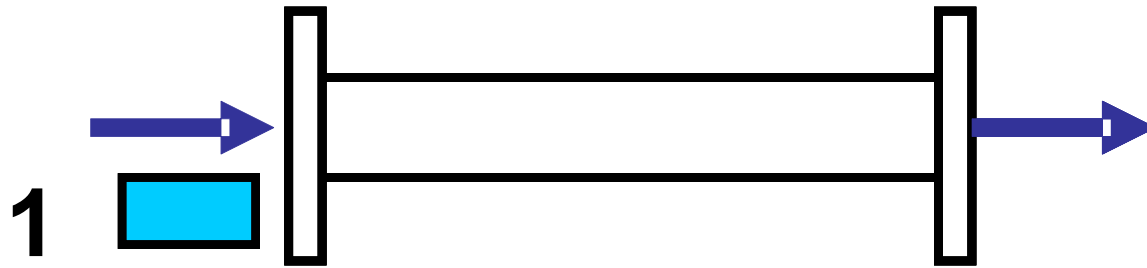
$2E$ [J]

Entropy

S [J/K]

$2S$ [J/K]

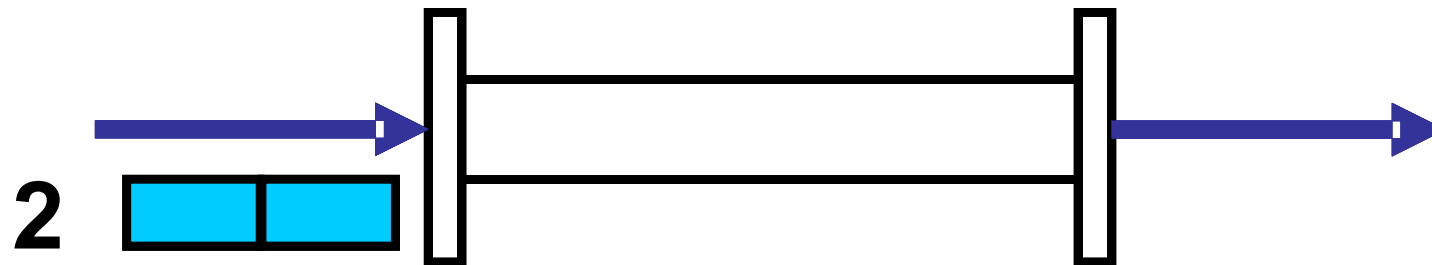
Ex. 2 Water flow into a tube (Continuous)



Energy
Entropy

E [J/s]
 S [J/(K·s)]

Same conditions
(Temperature, Pressure,
etc.)



Energy
Entropy

$2E$ [J/s]
 $2S$ [J/(K·s)]

Energy: E

▪ Volume changeable vessel:

Enthalpy H

▪ Constant volume vessel:

Internal energy U

What are energy and entropy?

Quantity of energy:

Enthalpy (Internal energy)

Quality of energy:

Expression by both enthalpy (Internal energy) and entropy



1) Calculation of enthalpy

Standard generation heat of material:

$$\Delta H^0_{298} \text{ [J/mol]}$$

Ex. CH ₄	-74.5 kJ/mol
C and N ₂	0 kJ/mol

(Pure material consisting of same element)

Enthalpy of material at temperature of T and the at atmospheric pressure: H^0_T

$$H^0_T = n\Delta H^0_{298} + n \int_{298}^T C_{p,m} dT$$

n : mol number of material [mol]

$C_{p,m}$: Heat capacity of material [J/(K·mol)]

$$C_{p,m} = a + bT + cT^2$$



2) Calculation of entropy

Absolute entropy of material: S^0_{298} [J/(K·mol)]

Ex. CH₄ 186 [J/(K·mol)]

Absolute entropy of material at temperature of T and at the atmospheric pressure: S^0_T

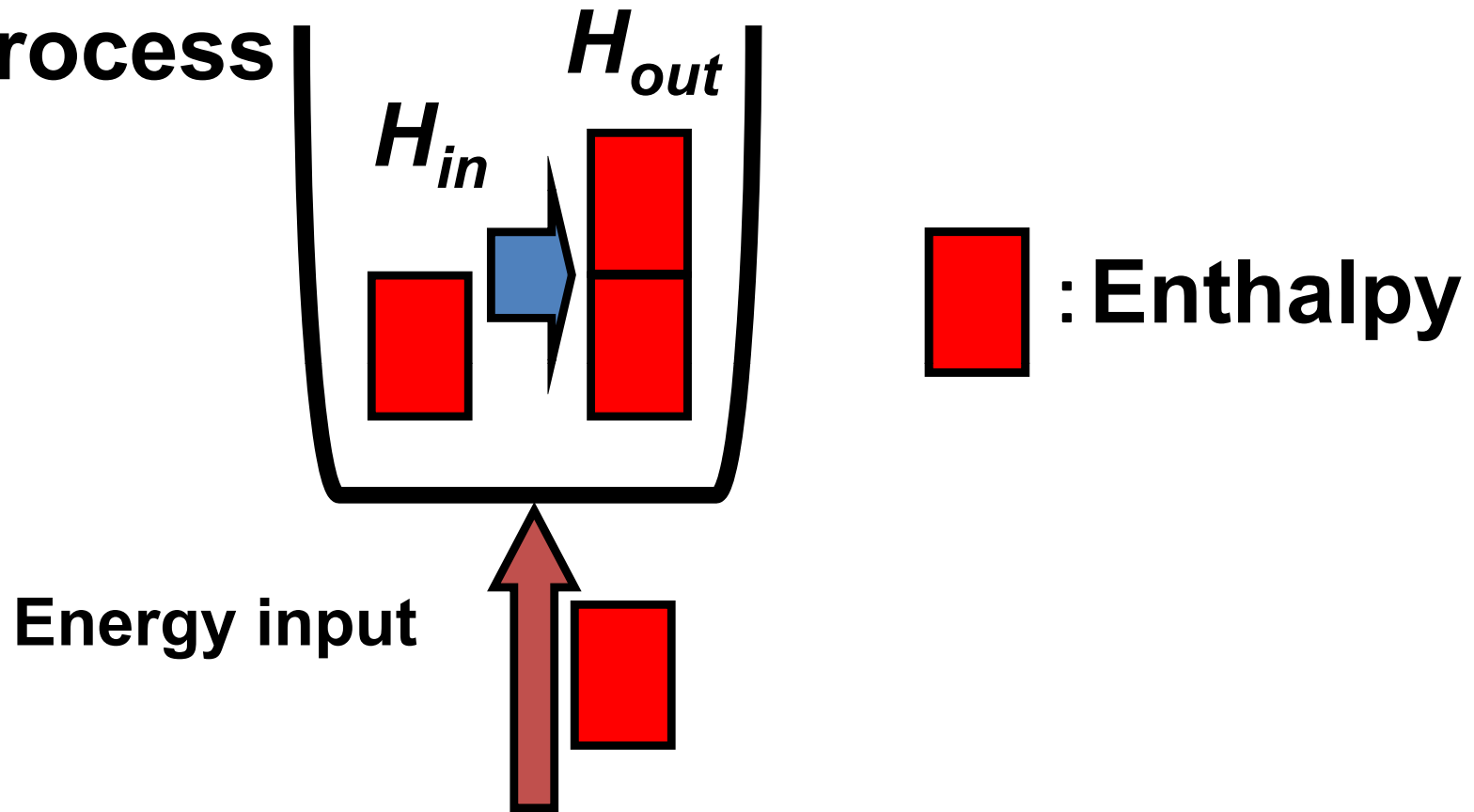
$$S^0_T = S^0_{298} + \int_{298}^T \frac{C_{p,m}}{T} dT$$



2) Thermodynamics for process

Ex. Heating process

- Batch process

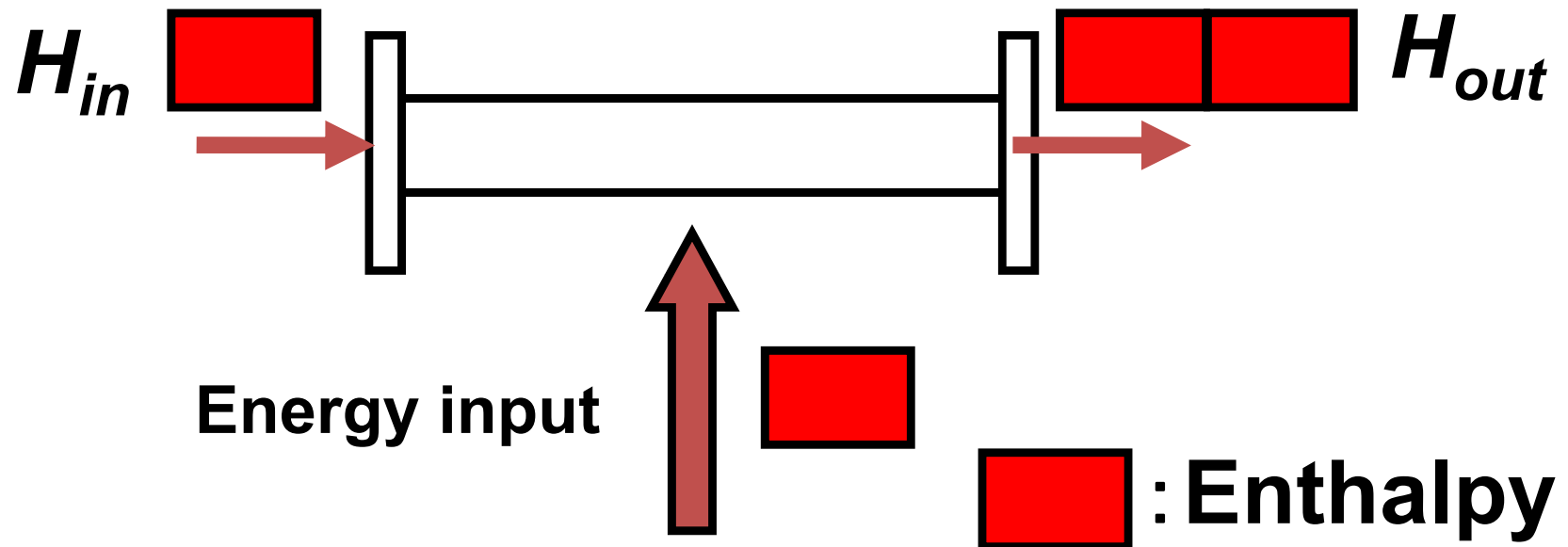


Enthalpy change before and after: ΔH

$$\Delta H = H_{out} - H_{in}$$

Ex. Heating process

- Continuous process

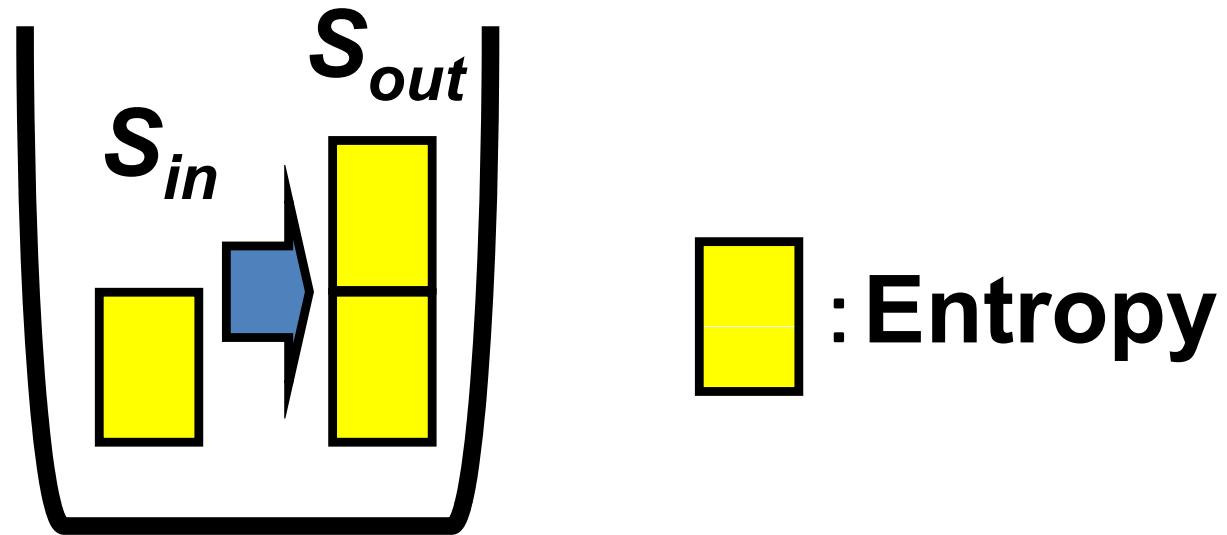


Enthalpy change before and after: ΔH

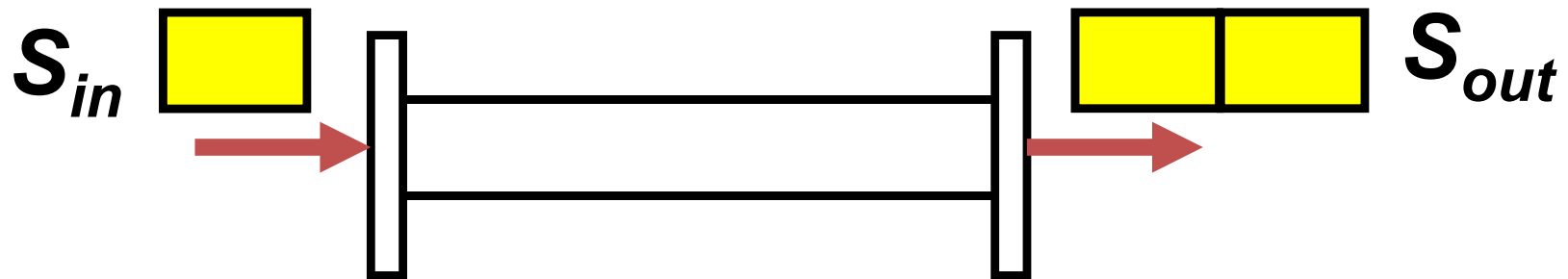
$$\Delta H = H_{out} - H_{in}$$

Ex. Heating process

▪ Batch process

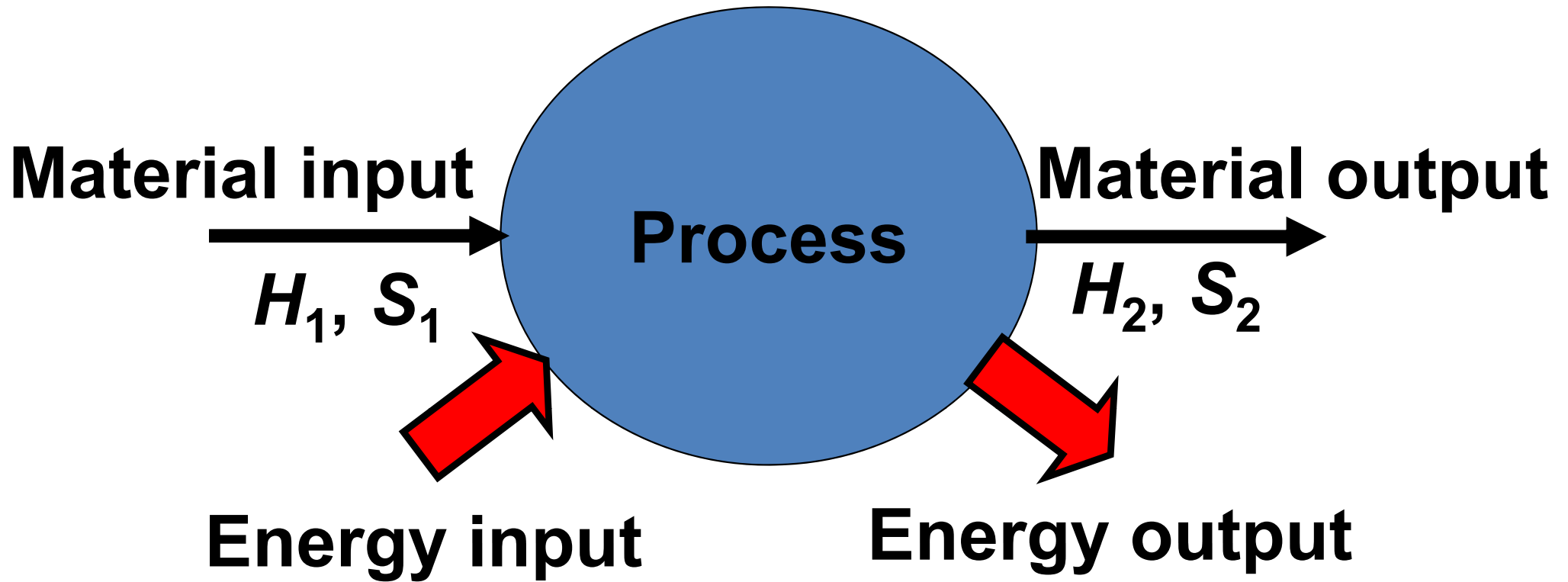


▪ Continuous process



Entropy change before and after: ΔS

$$\Delta S = S_{out} - S_{in}$$



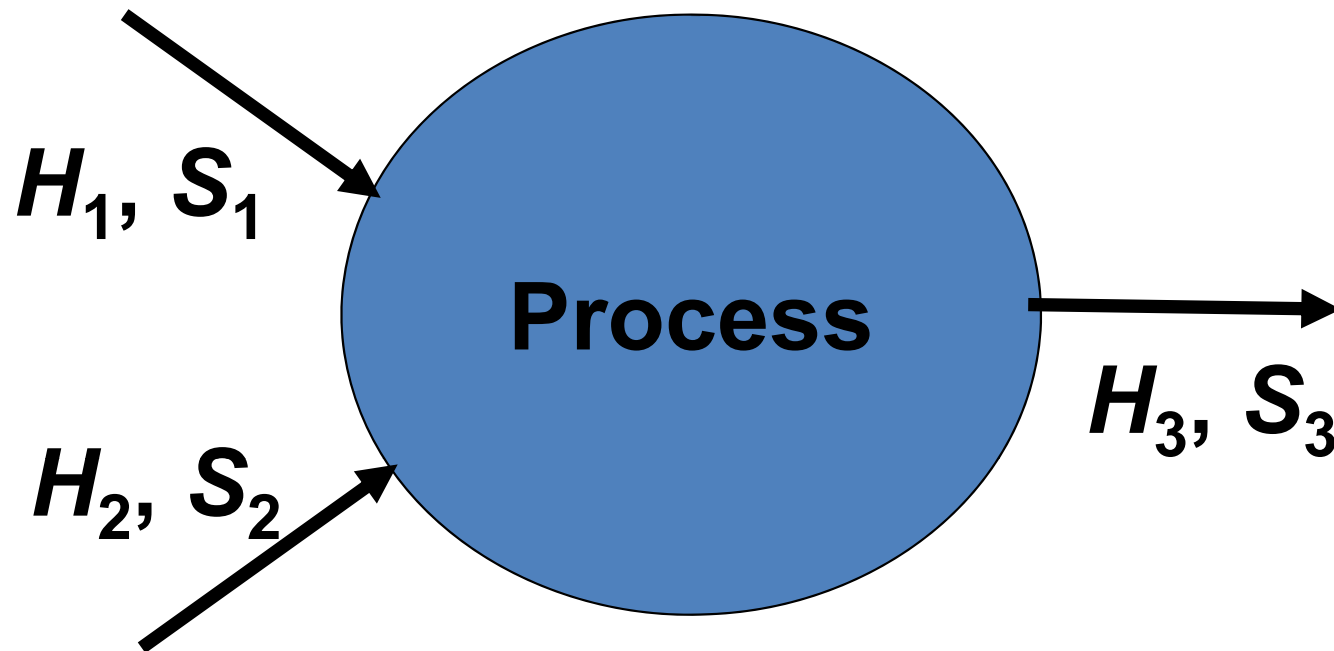
Enthalpy change  **: Intermediary energy**

$$\Delta H = \sum_j H_{out,j} - \sum_j H_{in,j}$$

Entropy change

$$\Delta S = \sum_j S_{out,j} - \sum_j S_{in,j}$$

E.g.



Enthalpy change

$$\Delta H = H_3 - (H_1 + H_2)$$

Entropy change

$$\Delta S = S_3 - (S_1 + S_2)$$

ΔH : Intermediary energy

ΔH : Intermediary energy

Direction: Positive or Negative of ΔH
(Positive: Energy input, Negative Energy output)

Quantity: Absolute value of ΔH

Quality: Degree of low level d

$$d = \frac{\Delta S}{\Delta H} \quad [1/K]$$

Degree of low level:

Larger d indicates lower intermediary energy.



What is the “Degree of low level”?

Assumption:

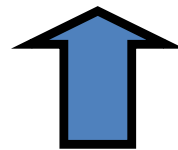
Evolution of 1 J intermediary energy

Temperature of heat source

1000K

300K

$$d \quad \mathbf{1/1000} < \mathbf{1/300}$$



Higher level of intermediary energy



Explanation of “Degree of low level” by Water model

Quantity of water = Mass of water

Degree of low level \longrightarrow Position of vessel

Position of vessel

0

1



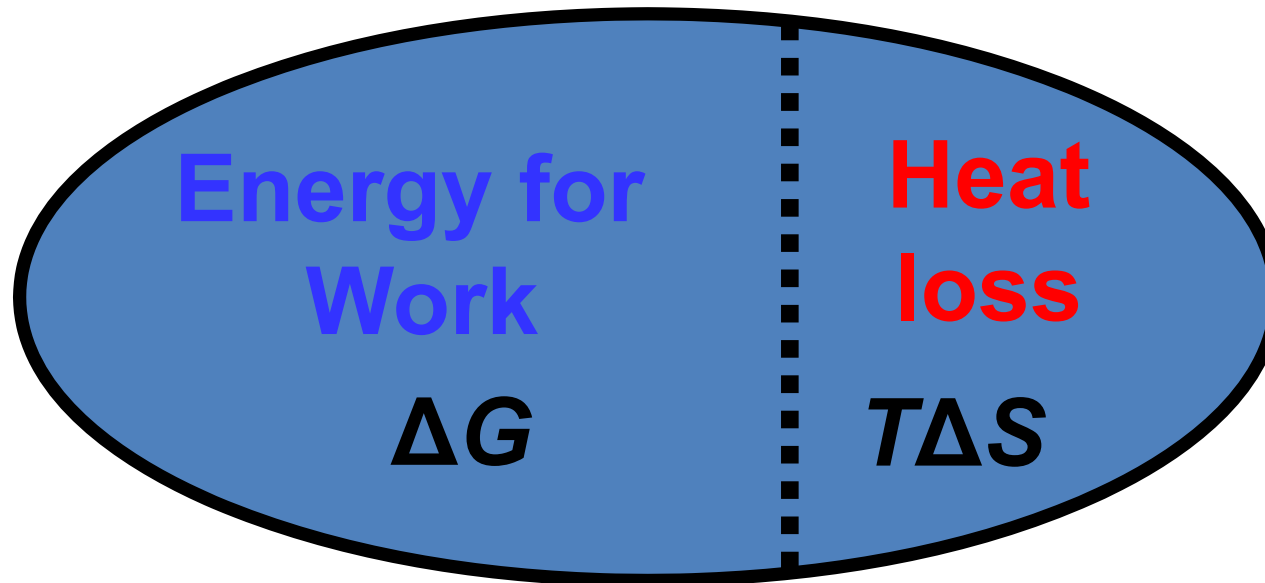
Before change

After change

Content of enthalpy change: ΔH

$$\Delta H = (\text{Energy for Work}) + (\text{Energy for thermodynamic heat loss})$$

Thermal energy which is Impossible to use
 ΔH



Change of Gibbs' free energy $\Delta G = \Delta H - T\Delta S$



Process	Quantity of energy	Temperature	ΔH	ΔS	Degree of low level d
Heat source	Output Q	T	$-Q$	$-Q/T$	$1/T$
Heat sink	Input Q	T	Q	Q/T	$1/T$
Work source	Output W	—	$-W$	0	0
Work sink	Input W	—	W	0	0

• Heat source and sink • • • No work function

$$\Delta G = 0$$

$$d = \frac{\Delta S}{\Delta H}$$

$$\Delta G = \Delta H - T\Delta S \quad \rightarrow \quad \Delta S = \Delta H / T$$

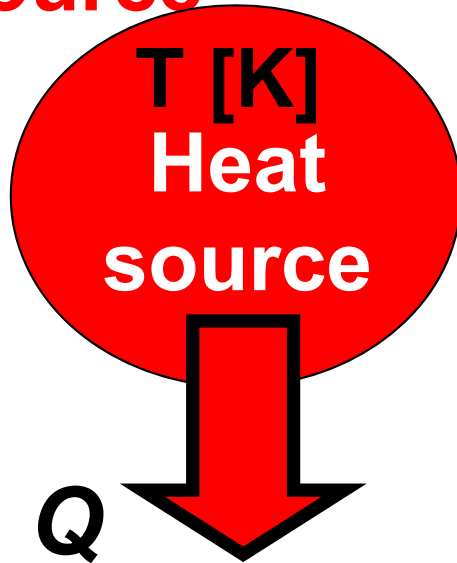
• Work source and sink • • • No thermal function

$$\Delta S = 0$$

Even if the Work source or sink evolves or takes energy, Respectively, the quality of them dose not change.



Heat source



$$\Delta H = -Q$$

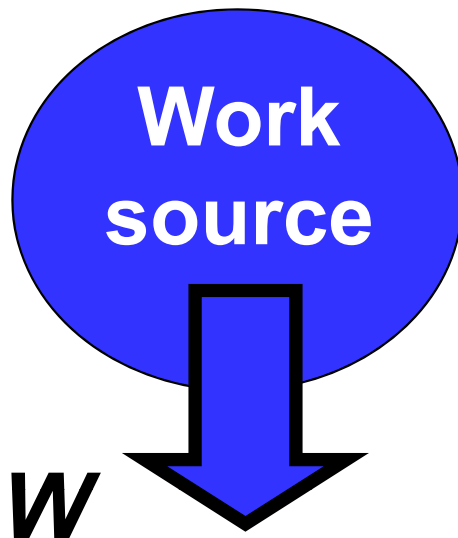
$$\Delta S = -Q/T$$

$$d = 1/T$$

$$\Delta S = \Delta H/T$$

$$d = \frac{\Delta S}{\Delta H}$$

Work source



$$\Delta H = -W$$

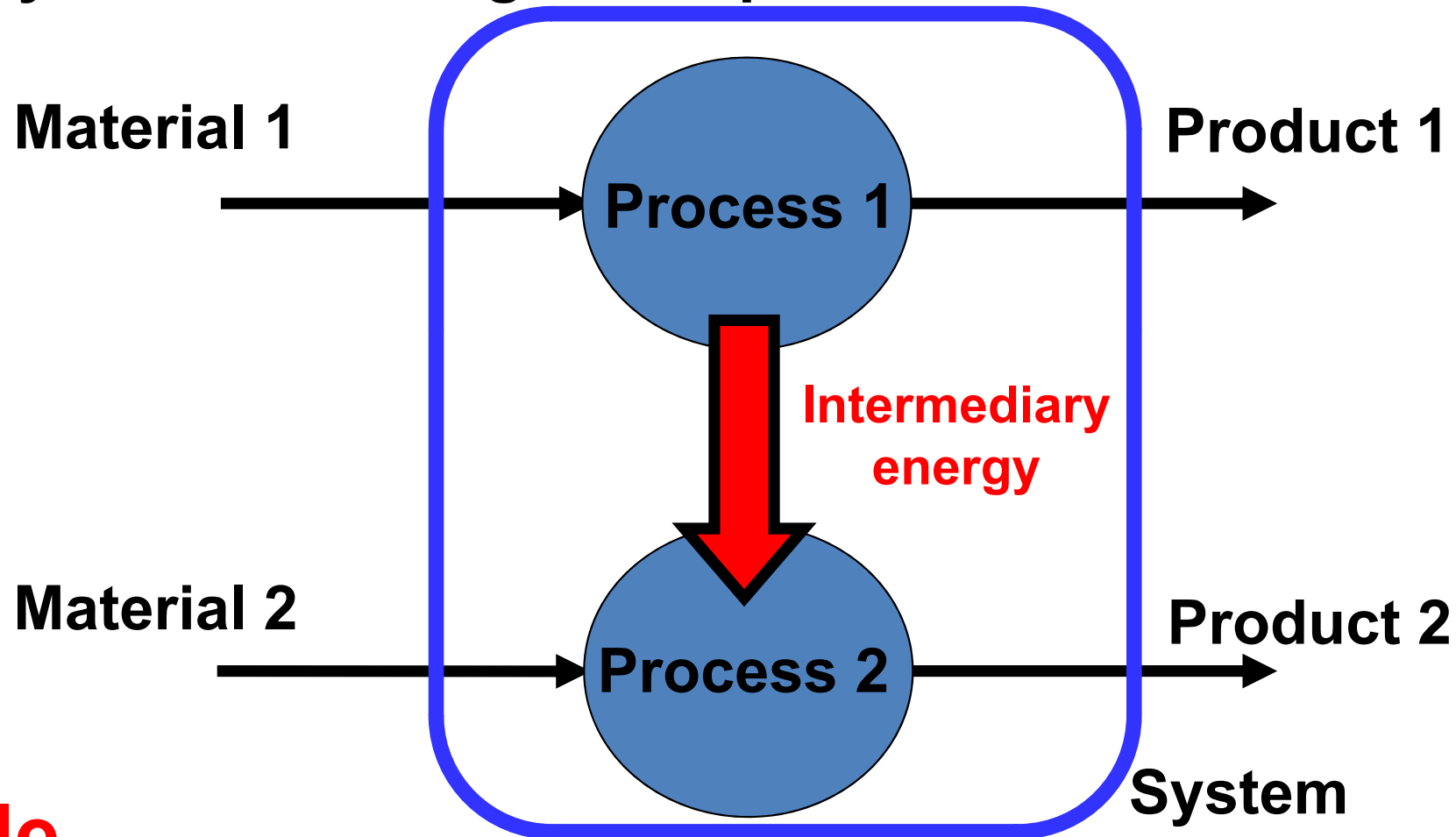
$$\Delta S = 0$$

$$d = 0$$

3) Thermodynamics for system

System: Assembly of processes

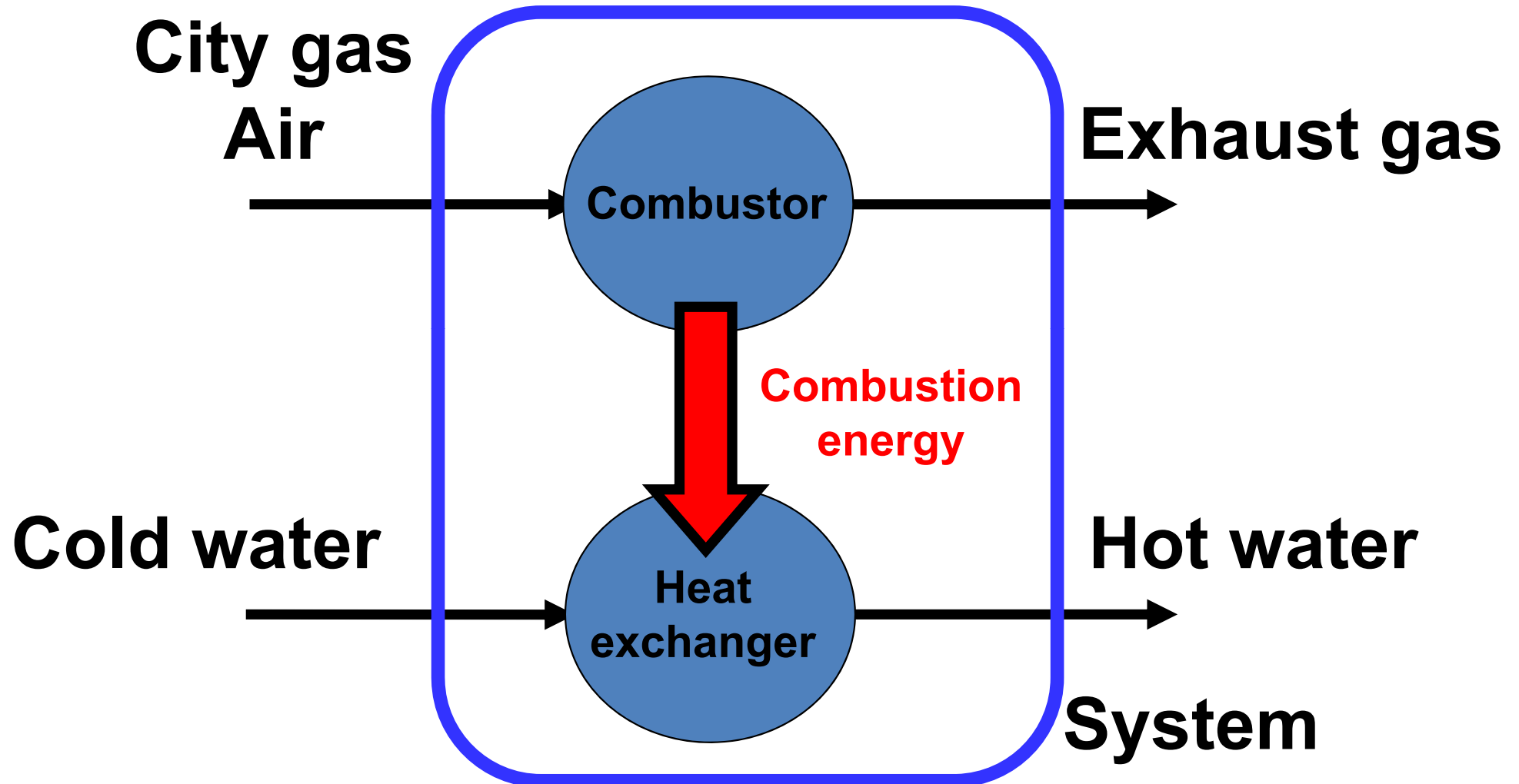
Ex. System consisting of two processes



Rule

The intermediary energy must not cross the system boundary.

Ex. Gas heating system for hot water



Thermodynamics for system

Rules

Only the materials can cross the system boundary.

The intermediary energy (Heat and Work) must not cross the system boundary.

The 1st law of thermodynamics

(Conservation law of energy)

$$\sum_j \Delta H_j = 0$$

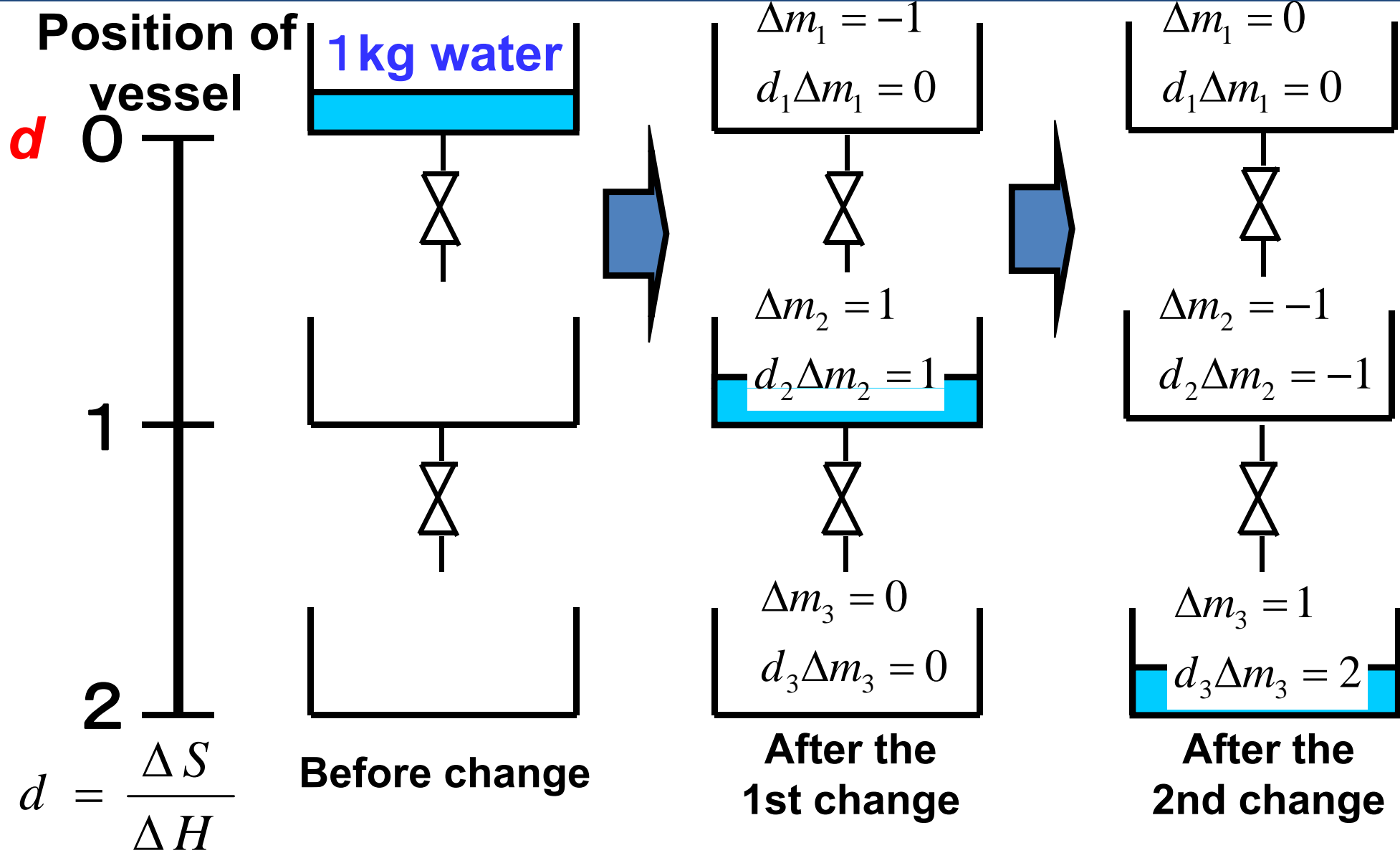
The 2nd law of thermodynamics

(Increase law of entropy)

$$\sum_j \Delta S_j \geq 0$$



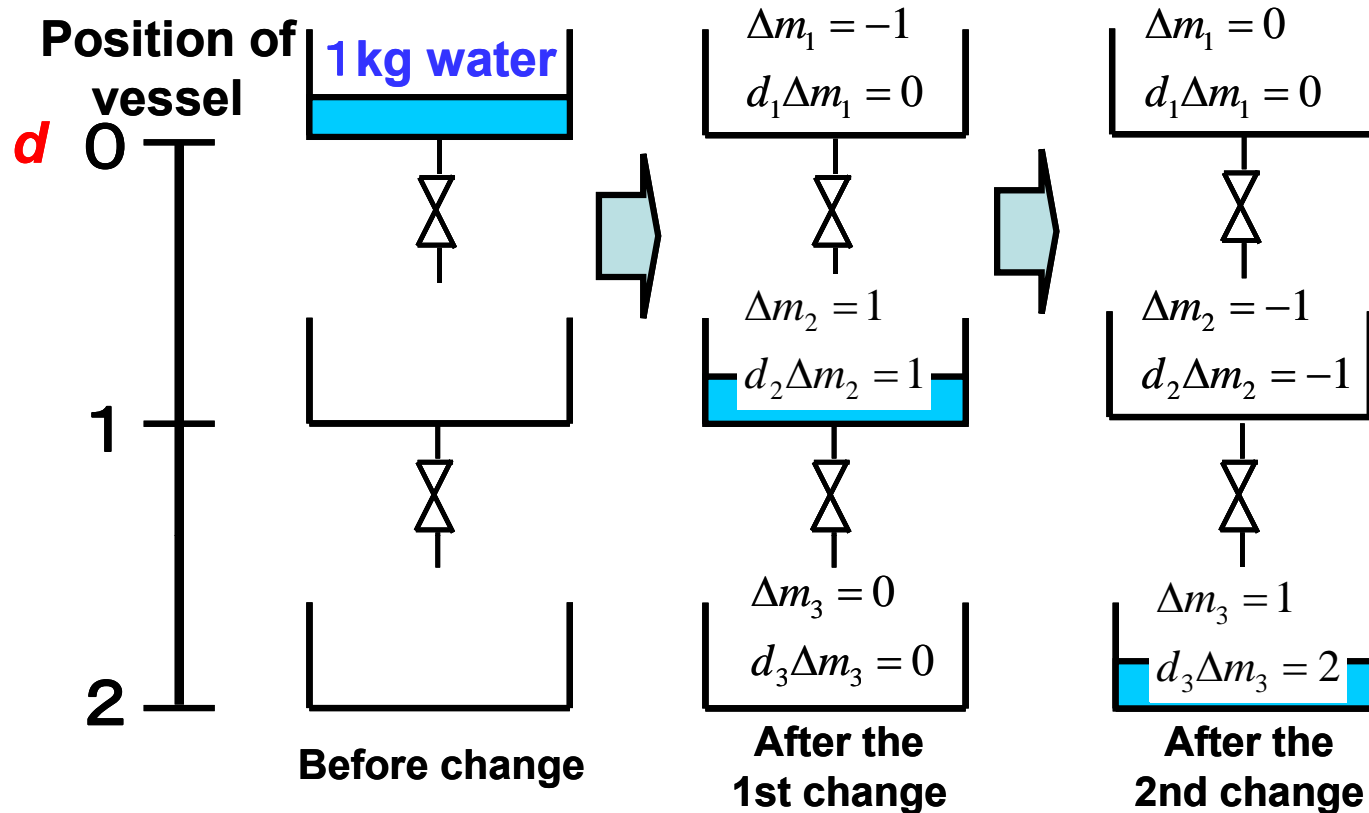
Explanation of the 1st and 2nd law of thermodynamics by Water model



$\Delta H \rightarrow$ Change of water mass : Δm

$d \rightarrow$ Position of water





The 1st law of thermodynamics (Conservation law of energy)

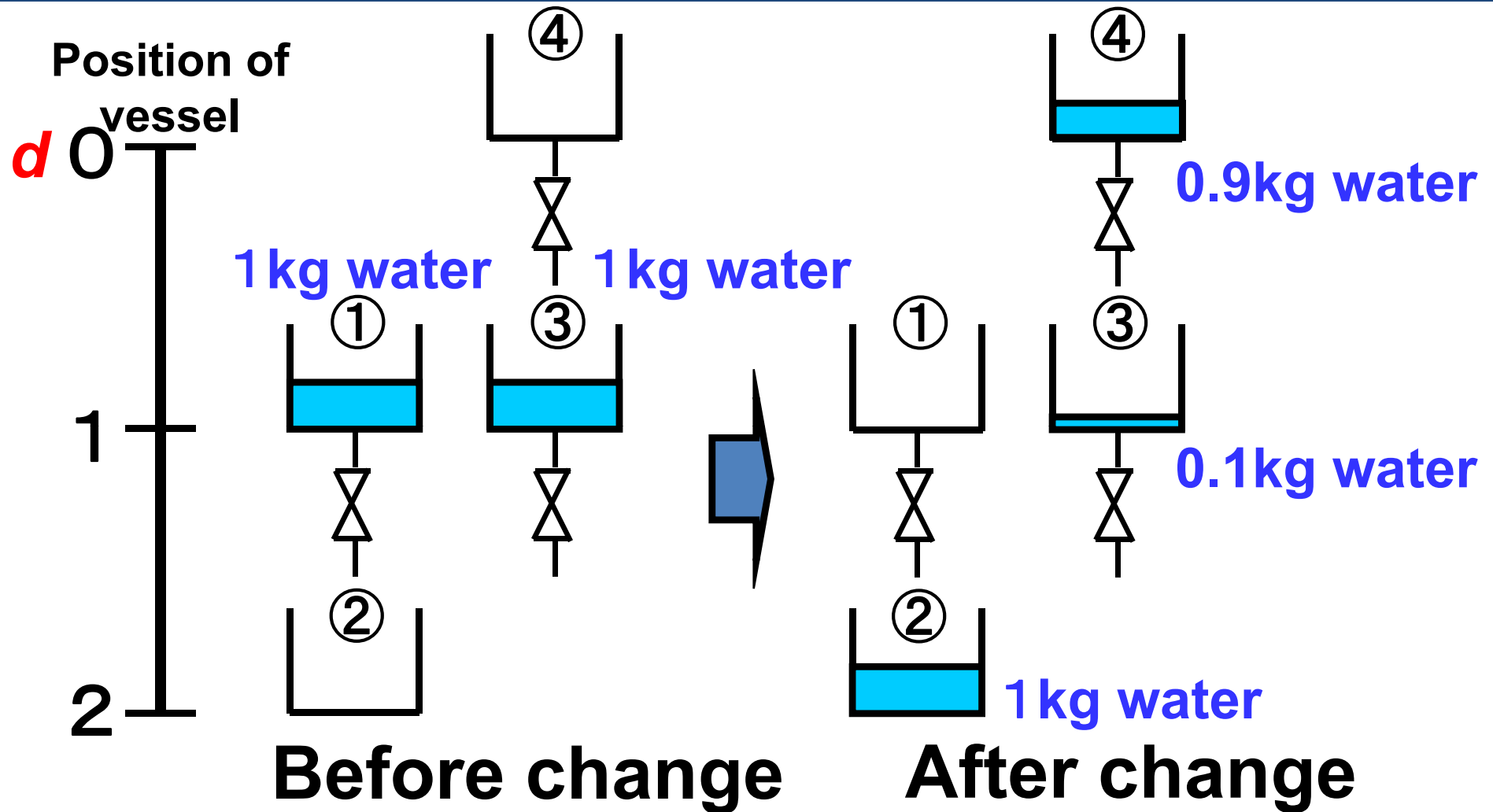
$$\sum_j \Delta H_j = \sum_j \Delta m_j = \Delta m_1 + \Delta m_2 + \Delta m_3 = 0$$

The 2nd law of thermodynamics (Increase law of entropy)

$$\sum_j \Delta S_j = \sum_j d_j \Delta m_j = d_1 \Delta m_1 + d_2 \Delta m_2 + d_3 \Delta m_3 = 1 \geq 0$$



Ex.

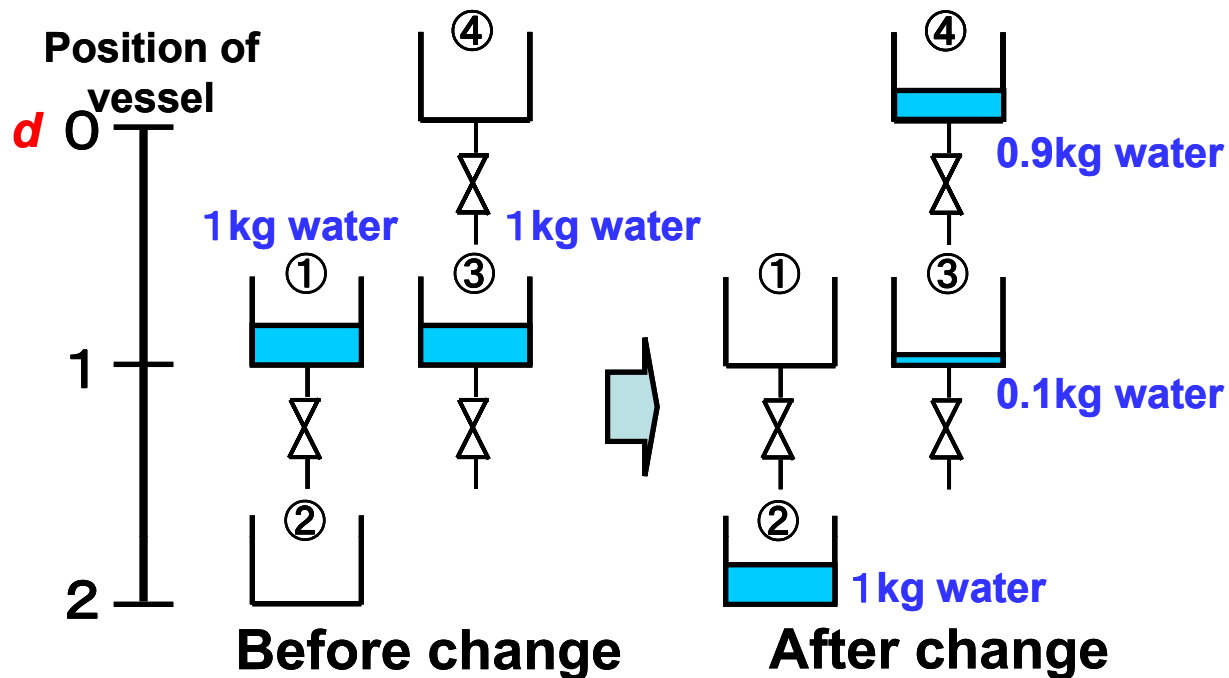


① $\Delta m_1 = -1, d_1 \Delta m_1 = -1$

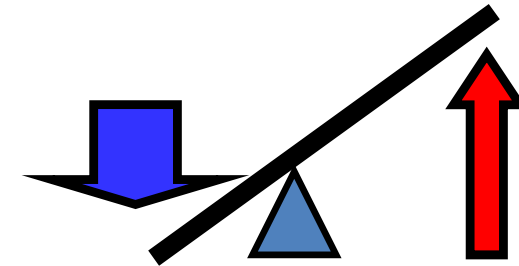
② $\Delta m_2 = 1, d_2 \Delta m_2 = 2$

③ $\Delta m_3 = -0.9, d_3 \Delta m_3 = -0.9$

④ $\Delta m_4 = 0.9, d_4 \Delta m_4 = 0$



Energy leverage



① $\Delta m_1 = -1, d_1 \Delta m_1 = -1$

② $\Delta m_2 = 1, d_2 \Delta m_2 = 2$

③ $\Delta m_3 = -0.9, d_3 \Delta m_3 = -0.9$

④ $\Delta m_4 = 0.9, d_4 \Delta m_4 = 0$

The 1st law of thermodynamics (Conservation law of energy)

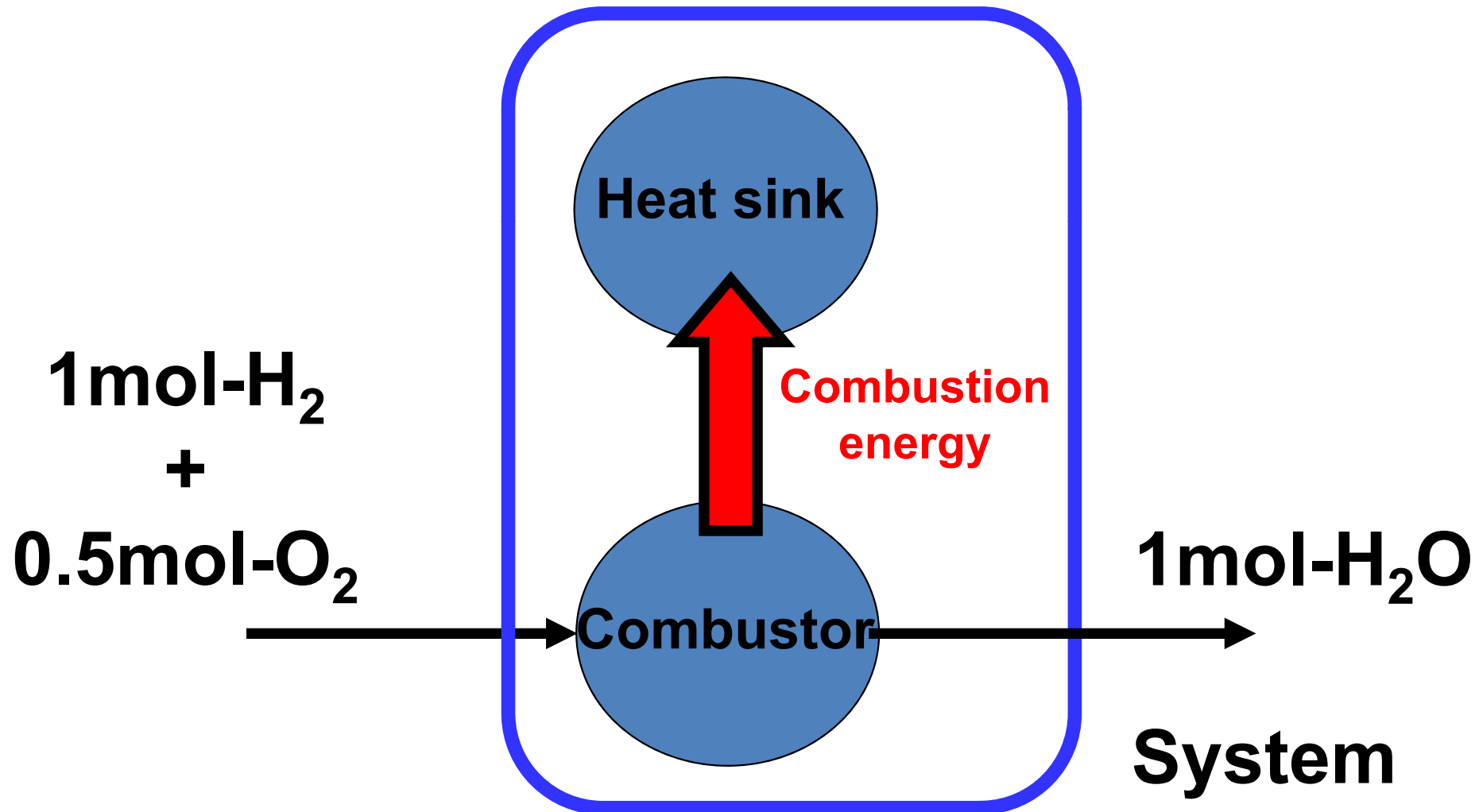
$$\sum_j \Delta H_j = \sum_j \Delta m_j = \Delta m_1 + \Delta m_2 + \Delta m_3 + \Delta m_4 = 0$$

The 2nd law of thermodynamics (Increase law of entropy)

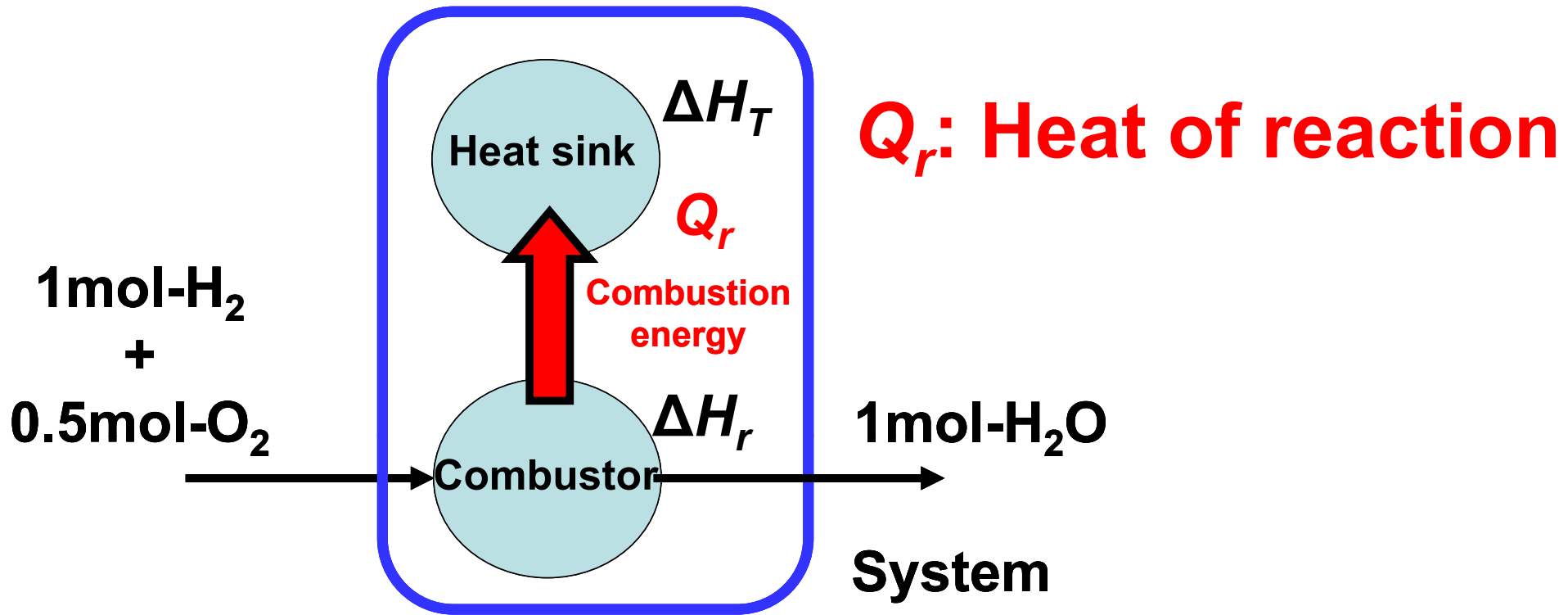
$$\sum_j \Delta S_j = \sum_j d_j \Delta m_j = d_1 \Delta m_1 + d_2 \Delta m_2 + d_3 \Delta m_3 + d_4 \Delta m_4 = 0.1 \geq 0$$

Applications of thermodynamics

Ex. Combustion of H₂ with O₂ $\text{H}_2 + 1/2\text{O}_2 \rightarrow \text{H}_2\text{O}$



Relationship between enthalpy change (ΔH_r) and reaction heat (Q_r)

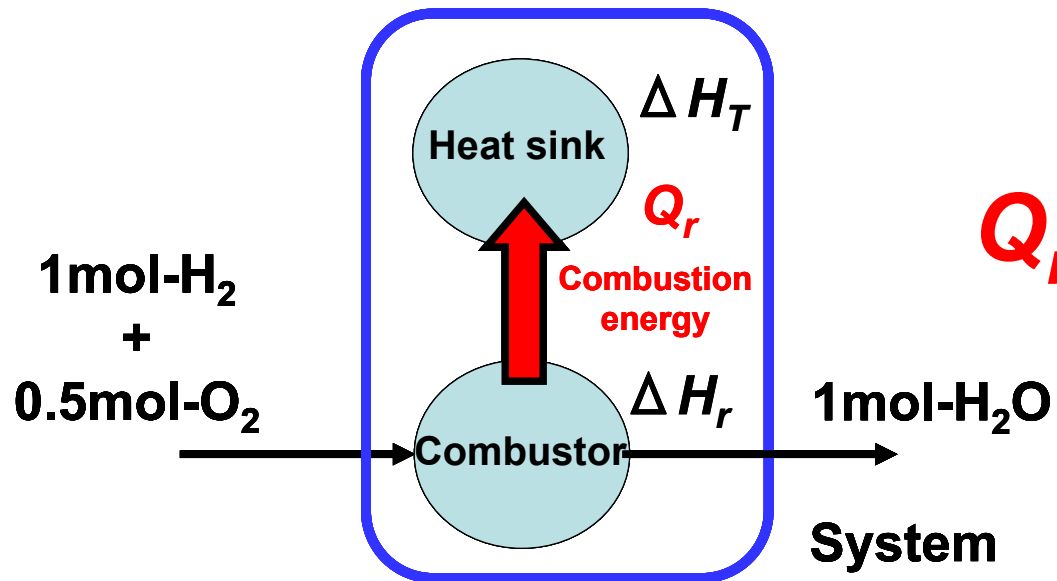


Energy change by reaction: ΔH_r

Energy change in heat sink: ΔH_T

From the 1st law $\Delta H_r + \Delta H_T = 0$

$$\Delta H_T = Q_r \longrightarrow \Delta H_r = -Q_r$$



Q_r : Heat of reaction

$$\Delta H_r = -Q_r$$

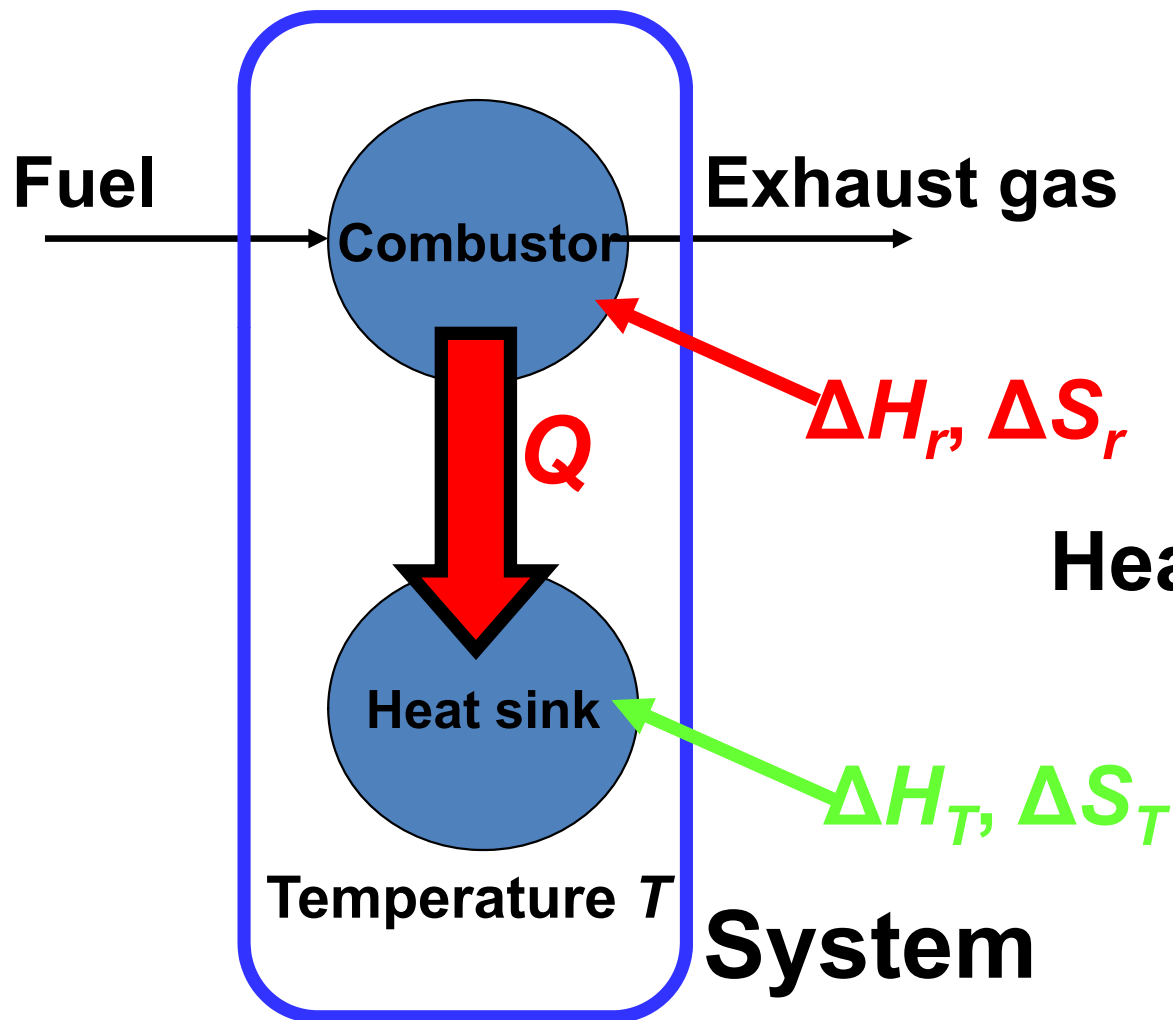
Exothermic reaction

$$Q_r > 0 \longrightarrow \Delta H_r : \text{Negative}$$

Endothermic reaction

$$Q_r < 0 \longrightarrow \Delta H_r : \text{Positive}$$

Exothermic reaction system



The 1st law

$$\Delta H_r + \Delta H_T = 0$$

The 2nd law

$$\Delta S_r + \Delta S_T \geq 0$$

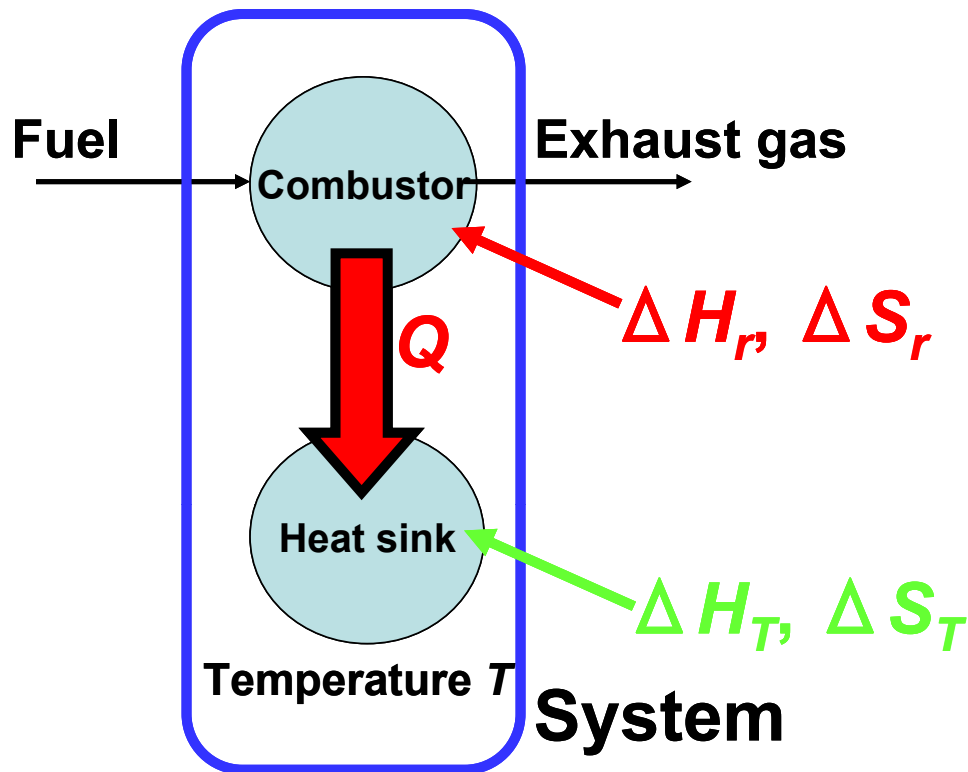
Heat sink

$$\Delta H_T = Q$$

$$\Delta S_T = Q/T \text{ より}$$

$$\Delta H_r + Q = 0$$

$$\Delta S_r + (Q/T) \geq 0$$



$$\Delta H_r + Q = 0$$

$$\Delta S_r + (Q/T) \geq 0$$



$$\Delta S_r - (\Delta H_r/T) \geq 0$$

Multiply $(-T)$ by both sides

$$\Delta H_r - T\Delta S_r \leq 0$$

Condition to occur exothermic reaction

$$\Delta H_r \leq T\Delta S_r$$

$$\Delta H - T\Delta S \equiv \Delta G$$

: Change of Gibbs' free energy

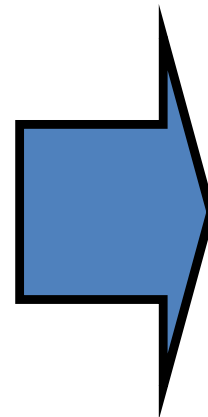
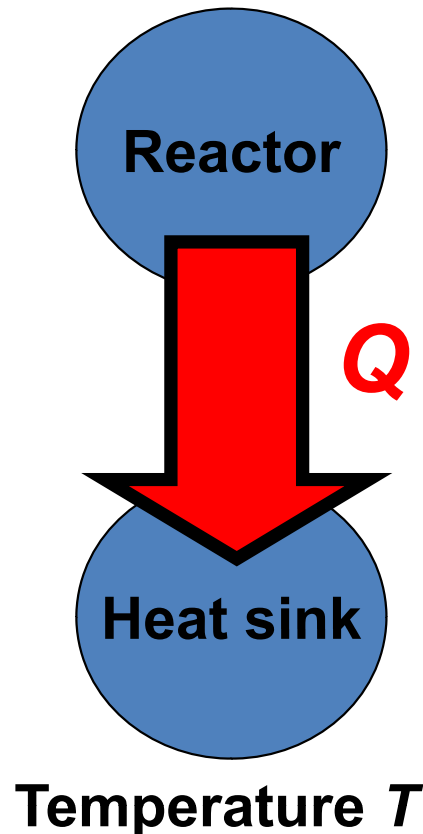
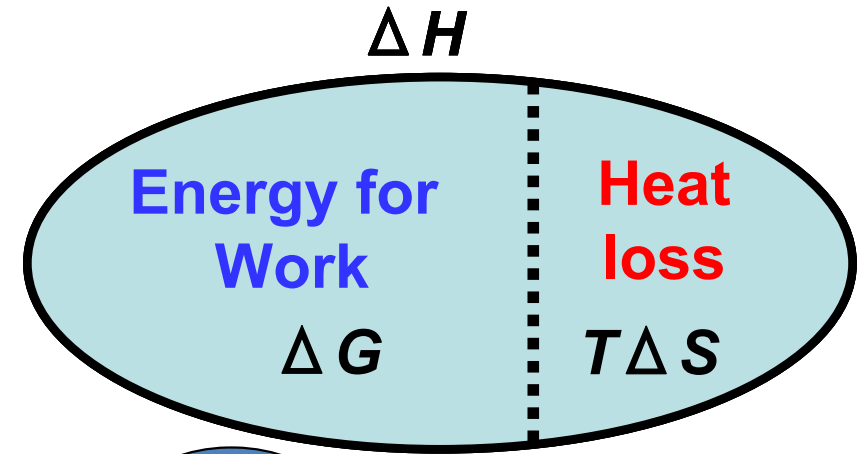
Condition to occur exothermic reaction

$$\Delta G_r \leq 0$$

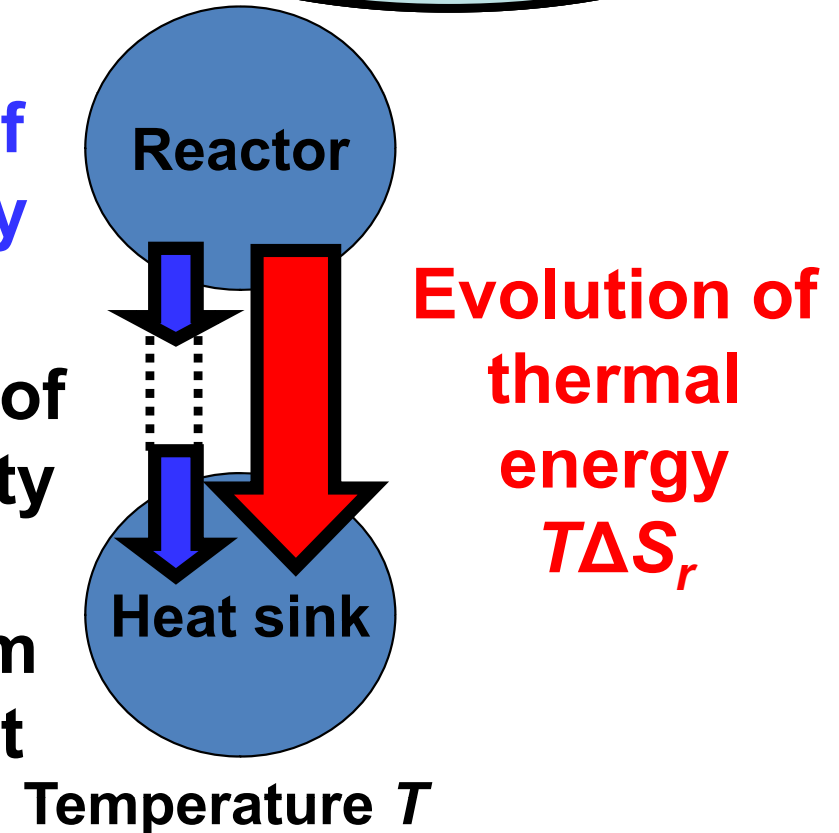


Content of enthalpy change: ΔH

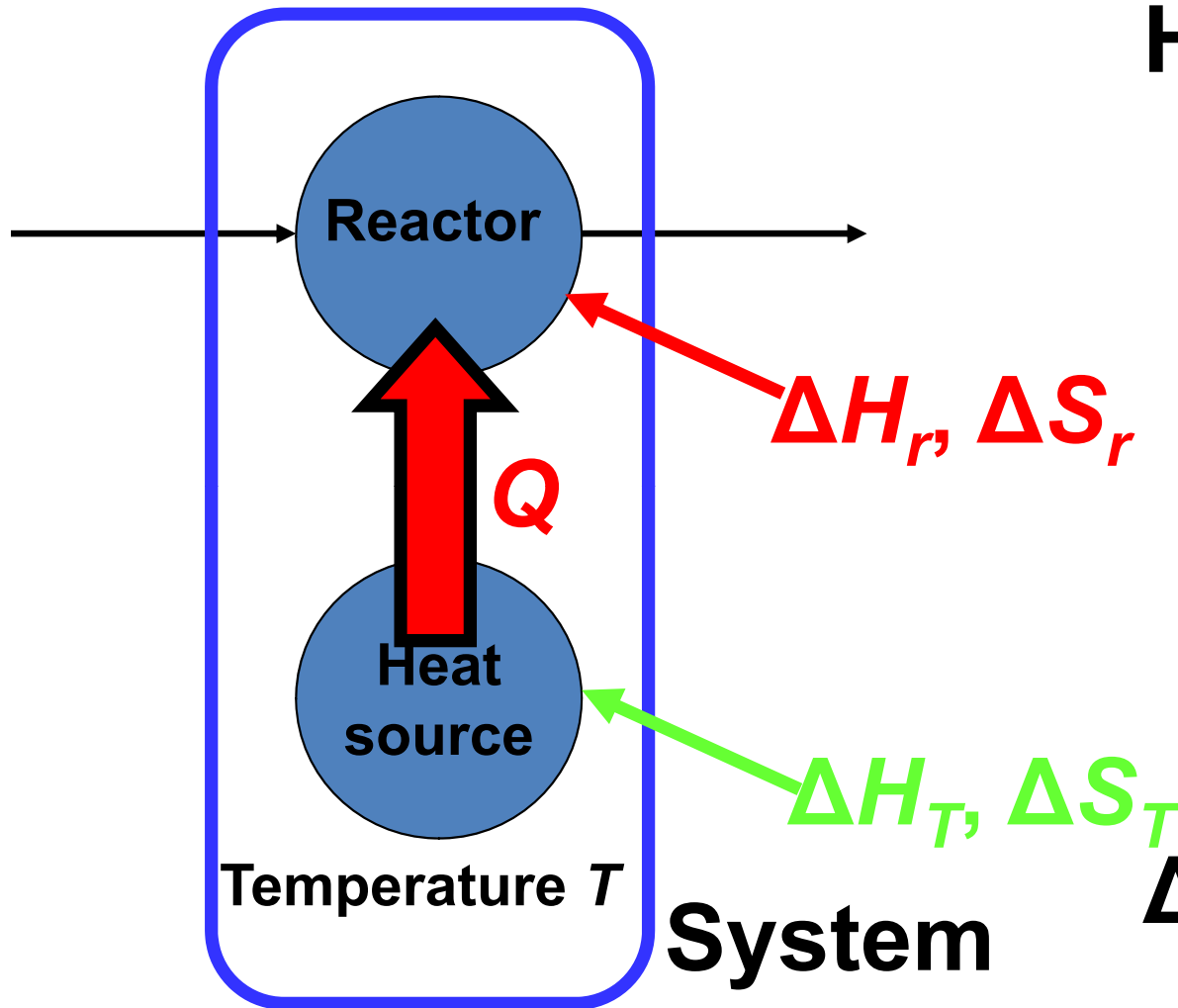
$$\Delta H = \Delta G + T\Delta S$$



Evolution of
work energy
 ΔG_r
Degradation of
energy quality
Convert from
work to heat



Endothermic reaction system



Heat source

$$\Delta H_T = -Q$$

$$\Delta S_T = -Q/T$$

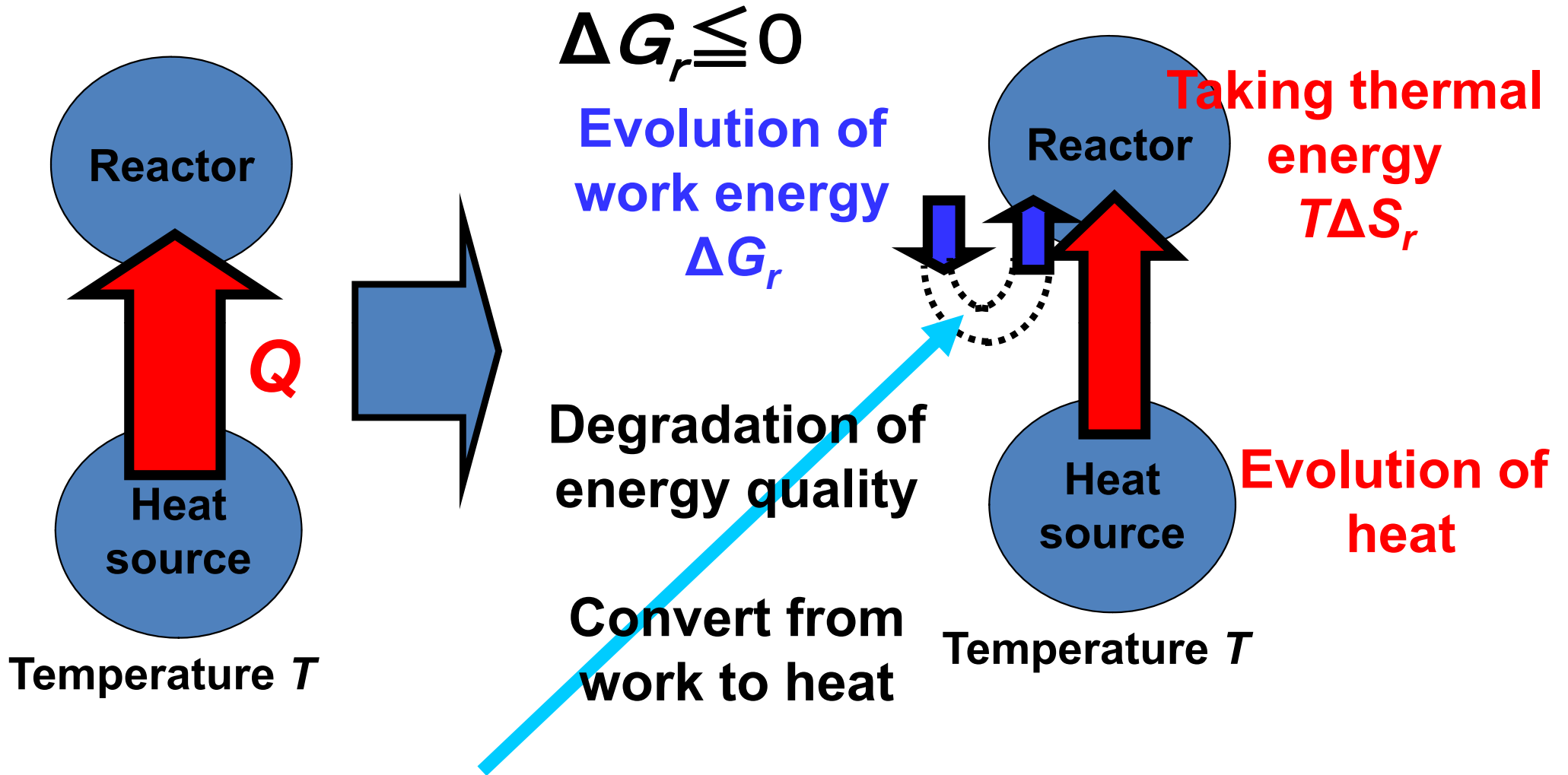
$$\Delta H_r - Q = 0$$

$$\Delta S_r - (Q/T) \geq 0$$

$$\Delta S_r - (\Delta H_r/T) \geq 0$$

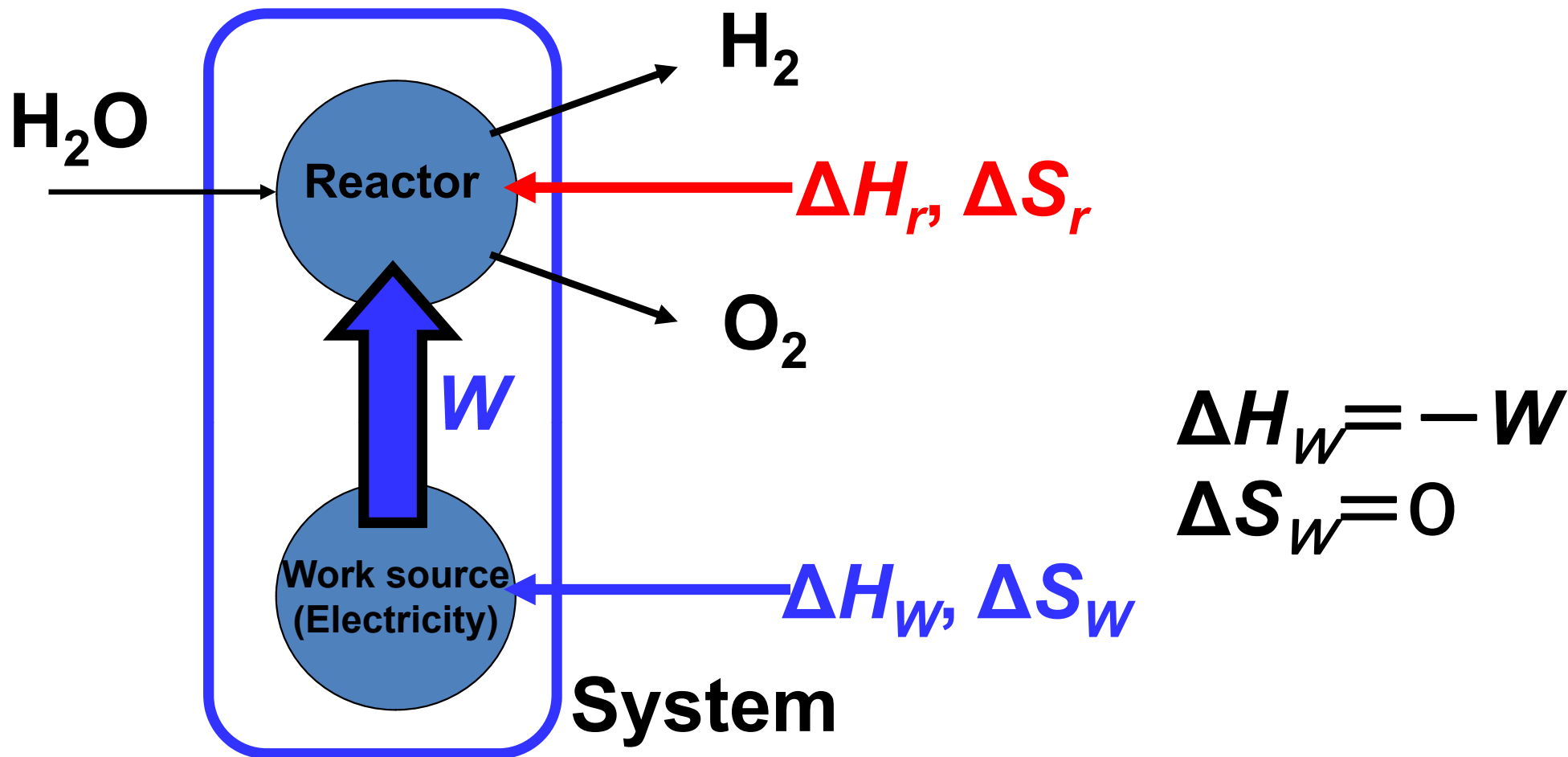
The condition for the endothermic reactions is the same as the for the exothermic reactions.

Endothermic reaction $\Delta H_r > 0$



Driving force for reaction

Ex. 1 Thermodynamic analysis of electric decomposition of water

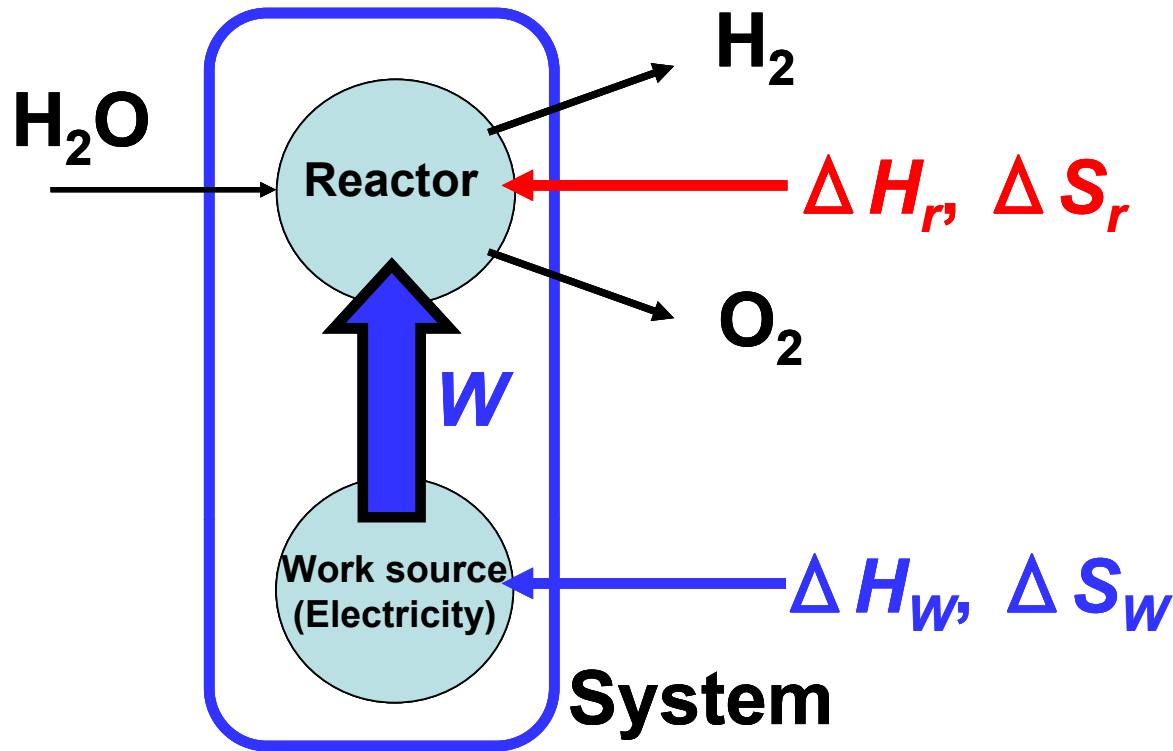


The 1st law $\Delta H_r + \Delta H_w = 0$

$\Delta H_r - W = 0$

The 2nd law $\Delta S_r + \Delta S_w \geq 0$

$\Delta S_r \geq 0$



$$\Delta H_r - W = 0$$

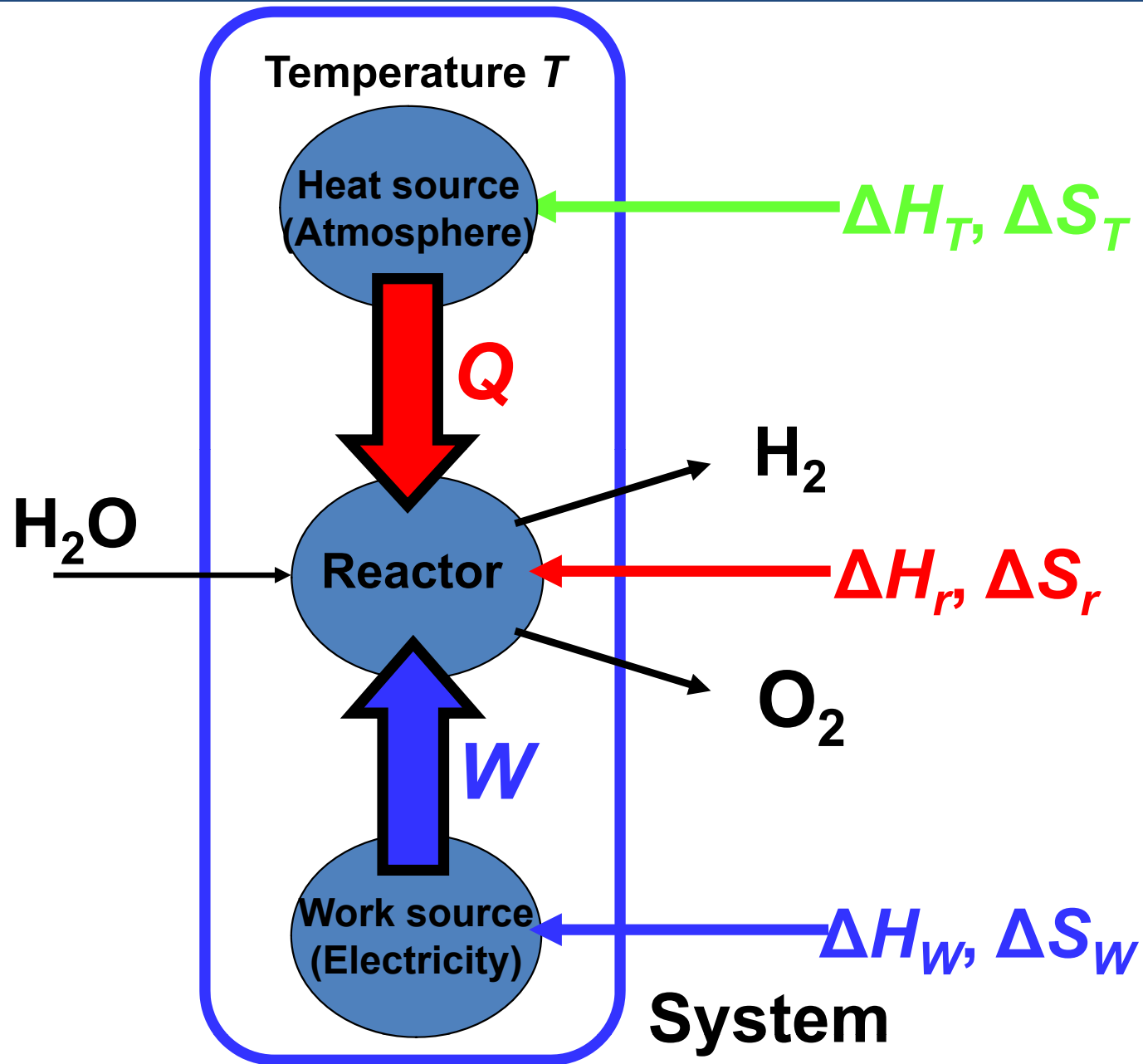


$$\Delta H_r = W$$

Experimental result $W \leq \Delta H_r$

Electric decomposition of water occurs by electric energy less than the theoretical heat of reaction.

Why?



The 1st law $\Delta H_r + \Delta H_w + \Delta H_T = 0$

The 2nd law $\Delta S_r + \Delta S_w + \Delta S_T \geq 0$

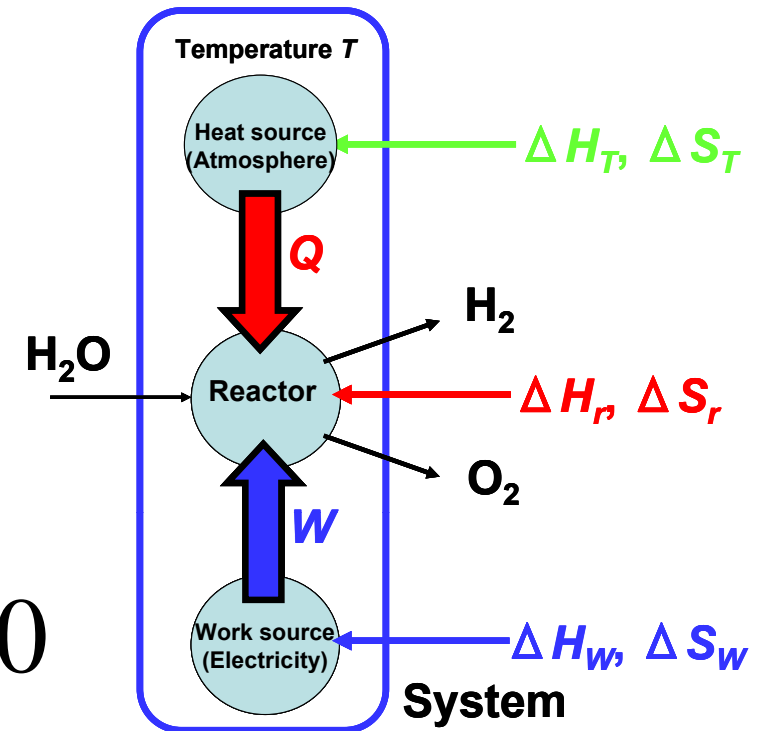
$$\Delta H_r - W - Q = 0$$

$$\Delta S_r - Q/T \geq 0$$

$$Q = \Delta H_r - W$$

$$\Delta S_r - \frac{\Delta H_r - W}{T} \geq 0$$

$$W \geq \Delta H_r - T\Delta S_r = \Delta G_r$$



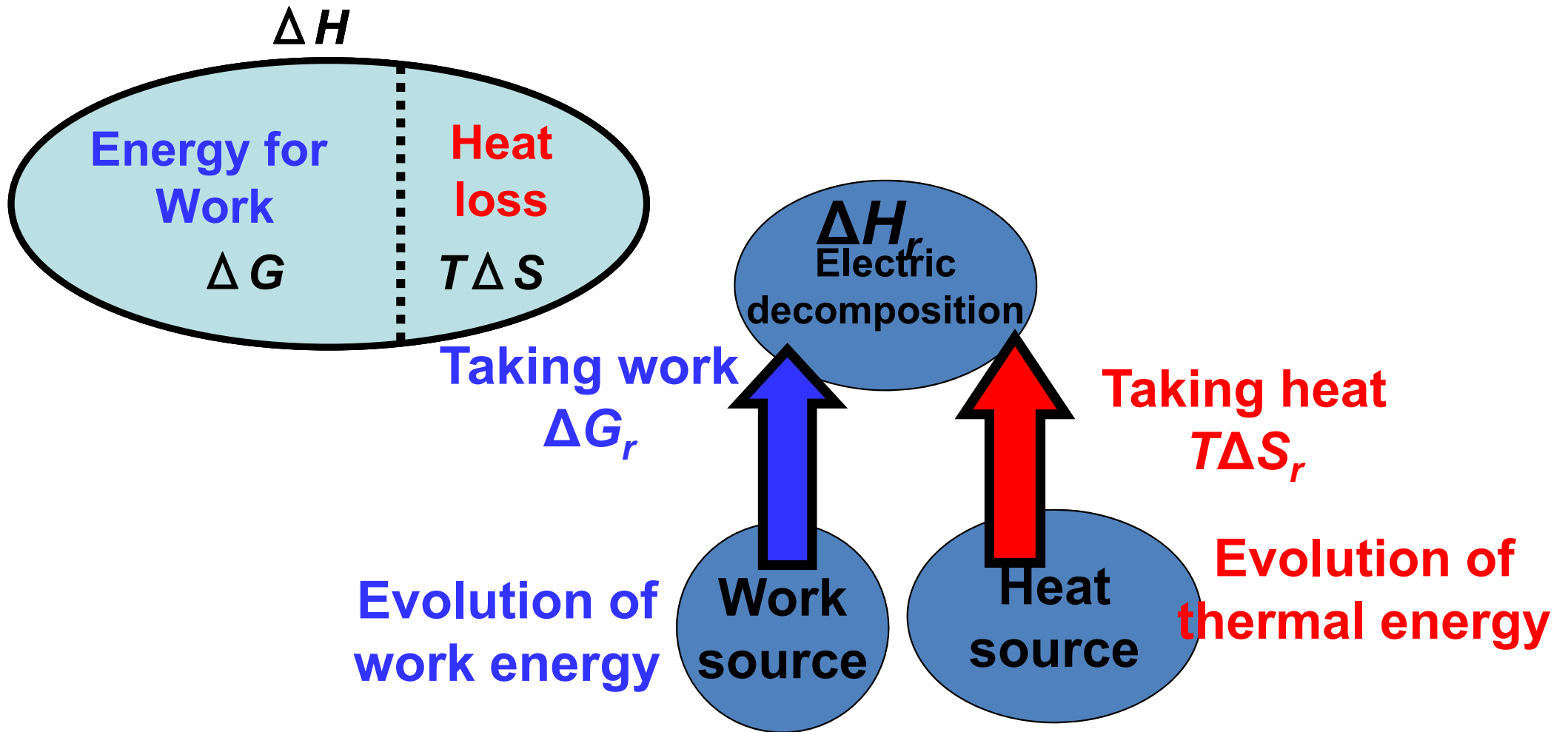
The reactor takes thermal energy of $T\Delta S_r$ from atmosphere.

Experimental results:

Consumed electricity \doteq Theoretical electricity

The electricity is reduced at high atmospheric temperature.





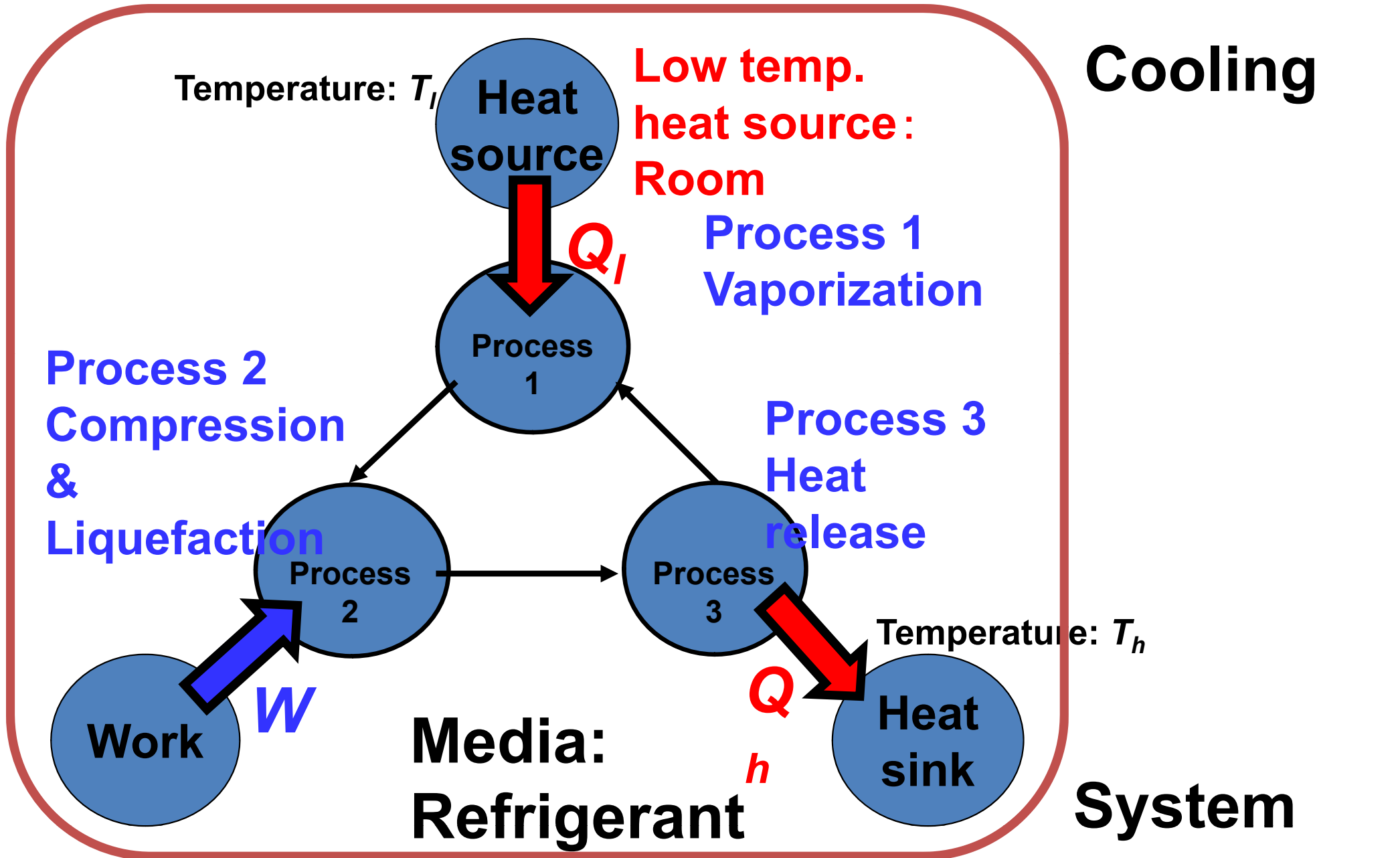
$$W = \Delta G_r$$

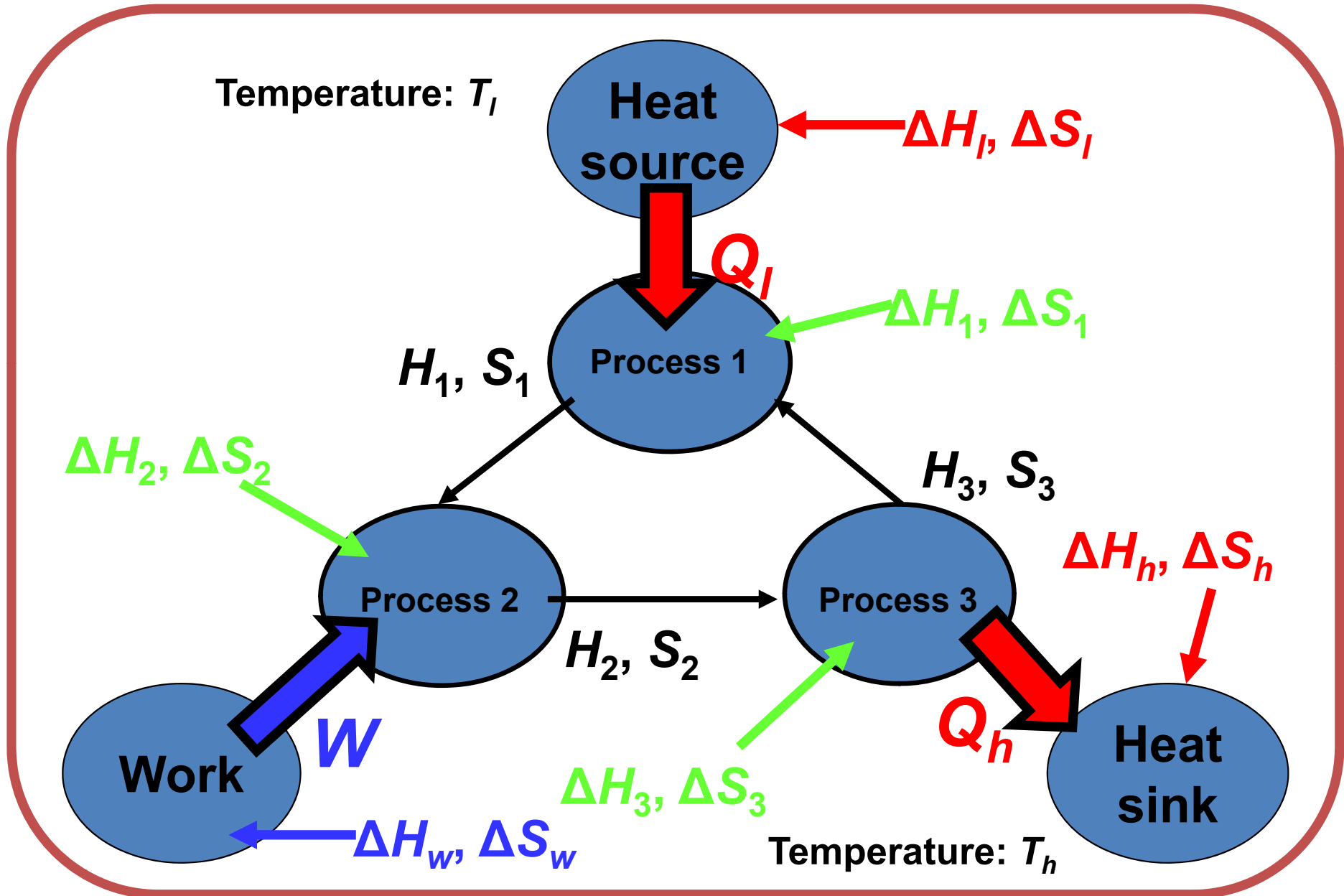
$$W > \Delta G_r$$

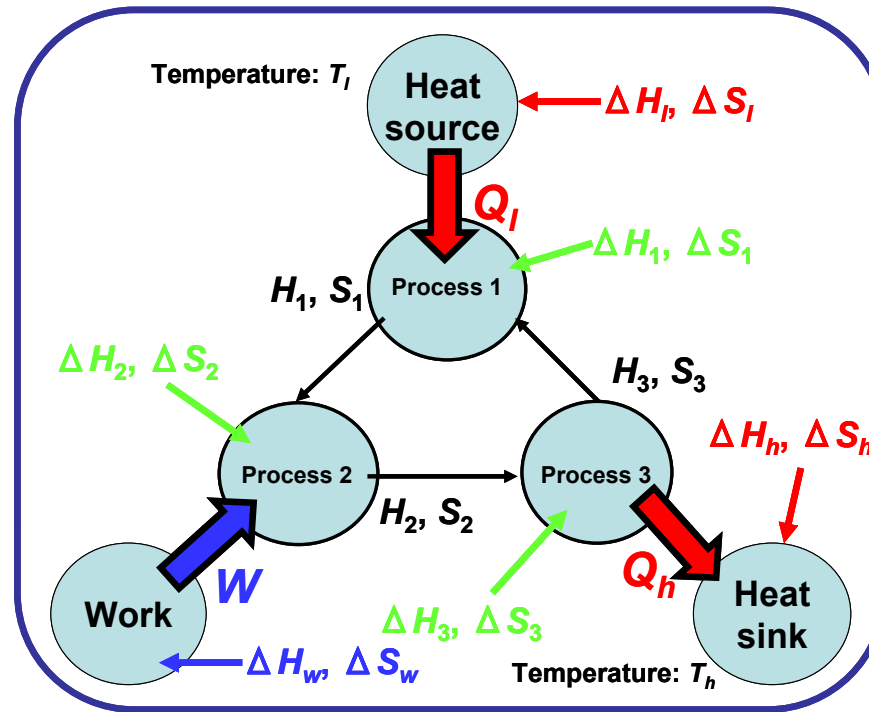
- **No degradation of intermediary energy**
- **Increase of electric energy and low thermal energy from heat sink**



Ex. 2 Thermodynamic analysis of heat pump





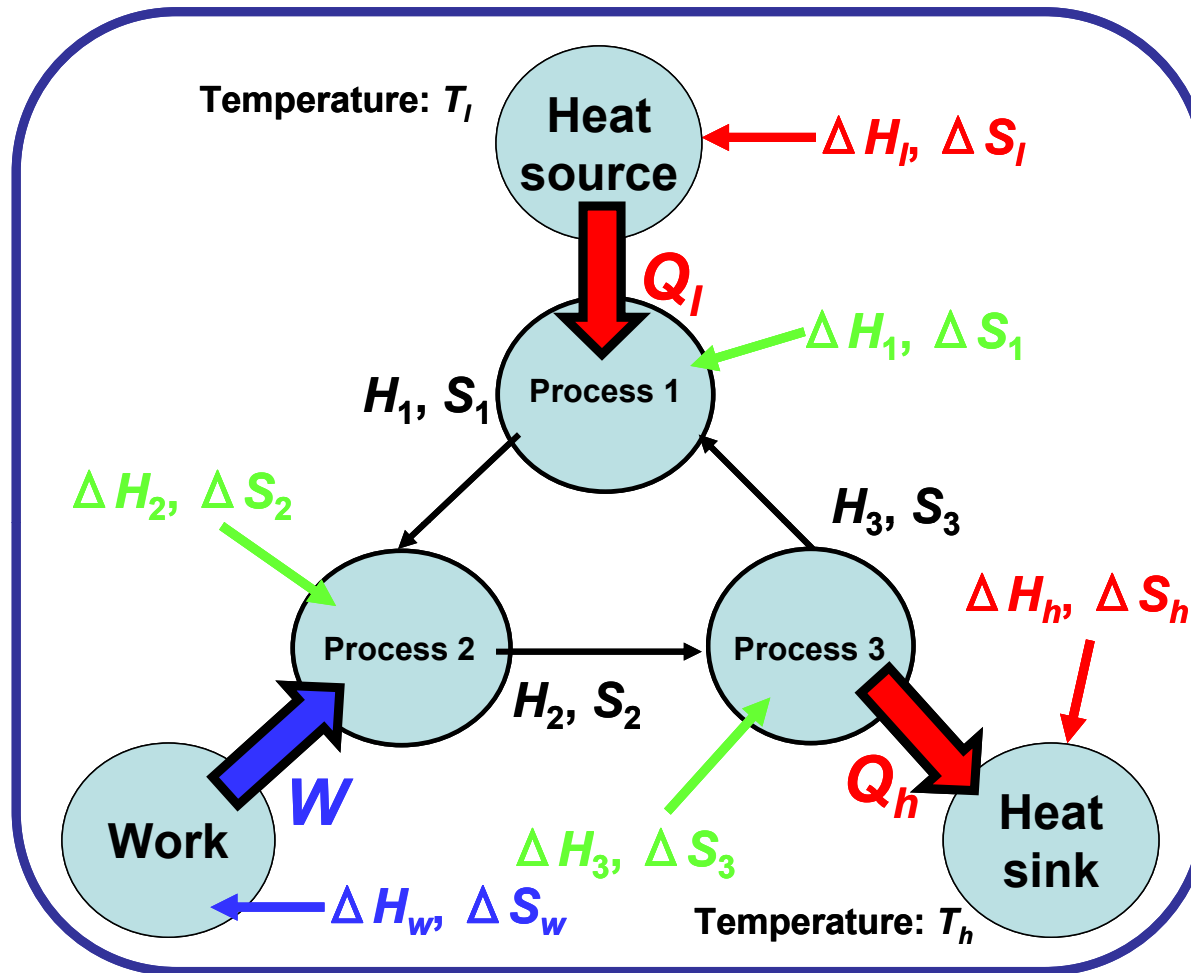


The 1st law
$$\underbrace{\Delta H_1 + \Delta H_2 + \Delta H_3}_{=0} + \Delta H_l + \Delta H_w + \Delta H_h = 0$$

The 2nd law
$$\underbrace{\Delta S_1 + \Delta S_2 + \Delta S_3}_{=0} + \Delta S_l + \Delta S_w + \Delta S_h \geq 0$$

$$\Delta H_1 + \Delta H_2 + \Delta H_3 = (H_1 - H_3) + (H_2 - H_1) + (H_3 - H_2) = 0$$

$$\Delta S_1 + \Delta S_2 + \Delta S_3 = (S_1 - S_3) + (S_2 - S_1) + (S_3 - S_2) = 0$$



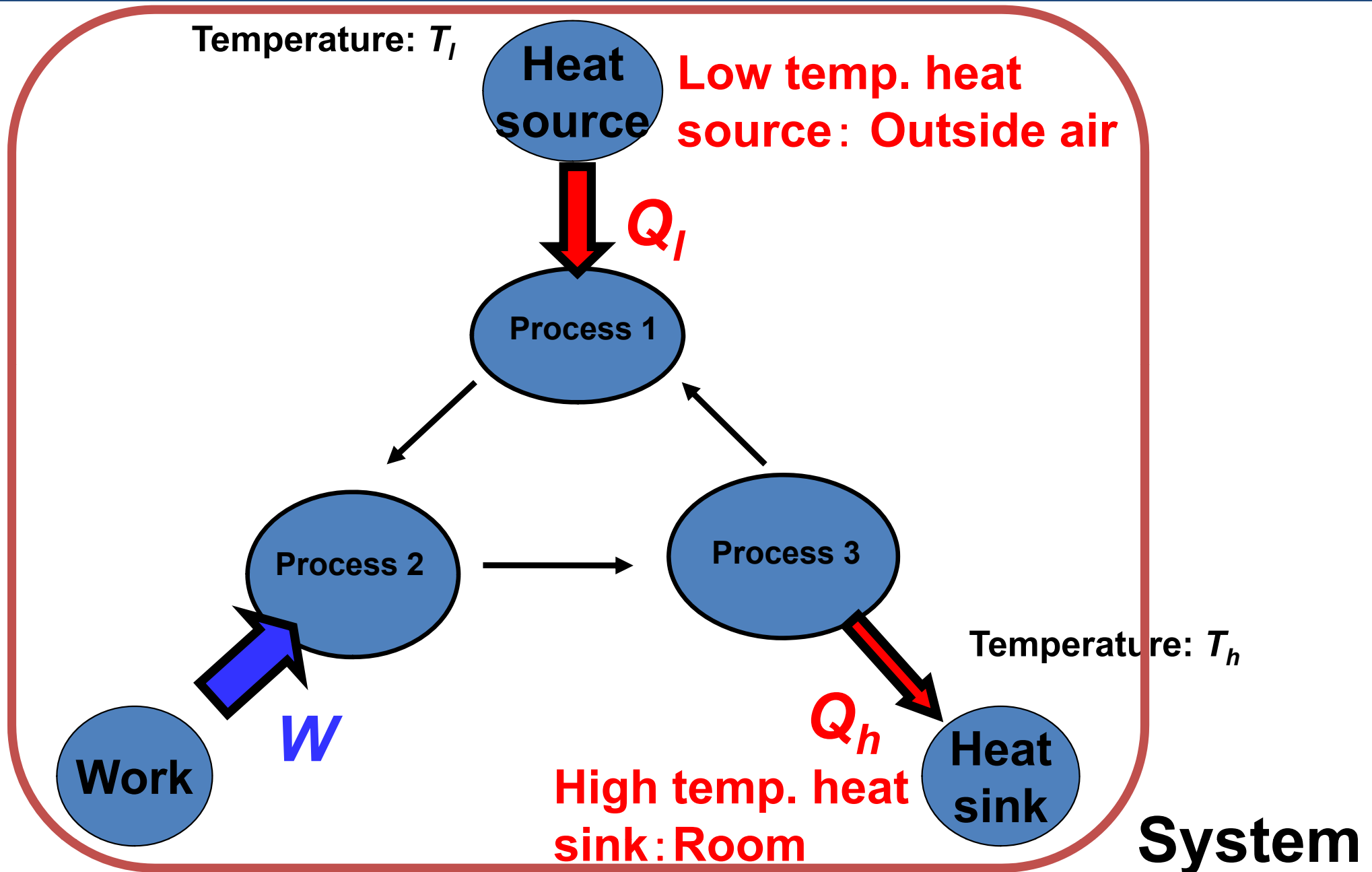
$$\Delta H_l + \Delta H_w + \Delta H_h = 0$$

$$-Q_l - W + Q_h = 0$$

$$\Delta S_l + \Delta S_w + \Delta S_h \geq 0$$

$$-\frac{Q_l}{T_l} + (0) + \frac{Q_h}{T_h} \geq 0$$

Room heating



Room heating

$$-Q_l - W + Q_h = 0 \quad -\frac{Q_l}{T_l} + \frac{Q_h}{T_h} \geq 0$$

$$Q_l = -W + Q_h$$

$$\frac{W - Q_h}{T_l} + \frac{Q_h}{T_h} \geq 0$$

$$W - Q_h + \frac{T_l}{T_h} Q_h \geq 0 \quad W \geq \frac{T_h - T_l}{T_h} Q_h$$

Cooling

$$W \geq \frac{T_h - T_l}{T_l} Q_l$$



Room heating

$$W \geq \frac{T_h - T_l}{T_h} Q_h$$

Heat at T_l in the air is taken. $T_h > T_l$

The room at T_h is heated at heating rate of Q_h .

Ex. Outside temp.: $-3^\circ\text{C}(=270\text{K})$

Room temp.: $27^\circ\text{C}(=300\text{K})$

Heating rate = $1\text{ kW} = (1\text{ kJ/s}) = Q_h$

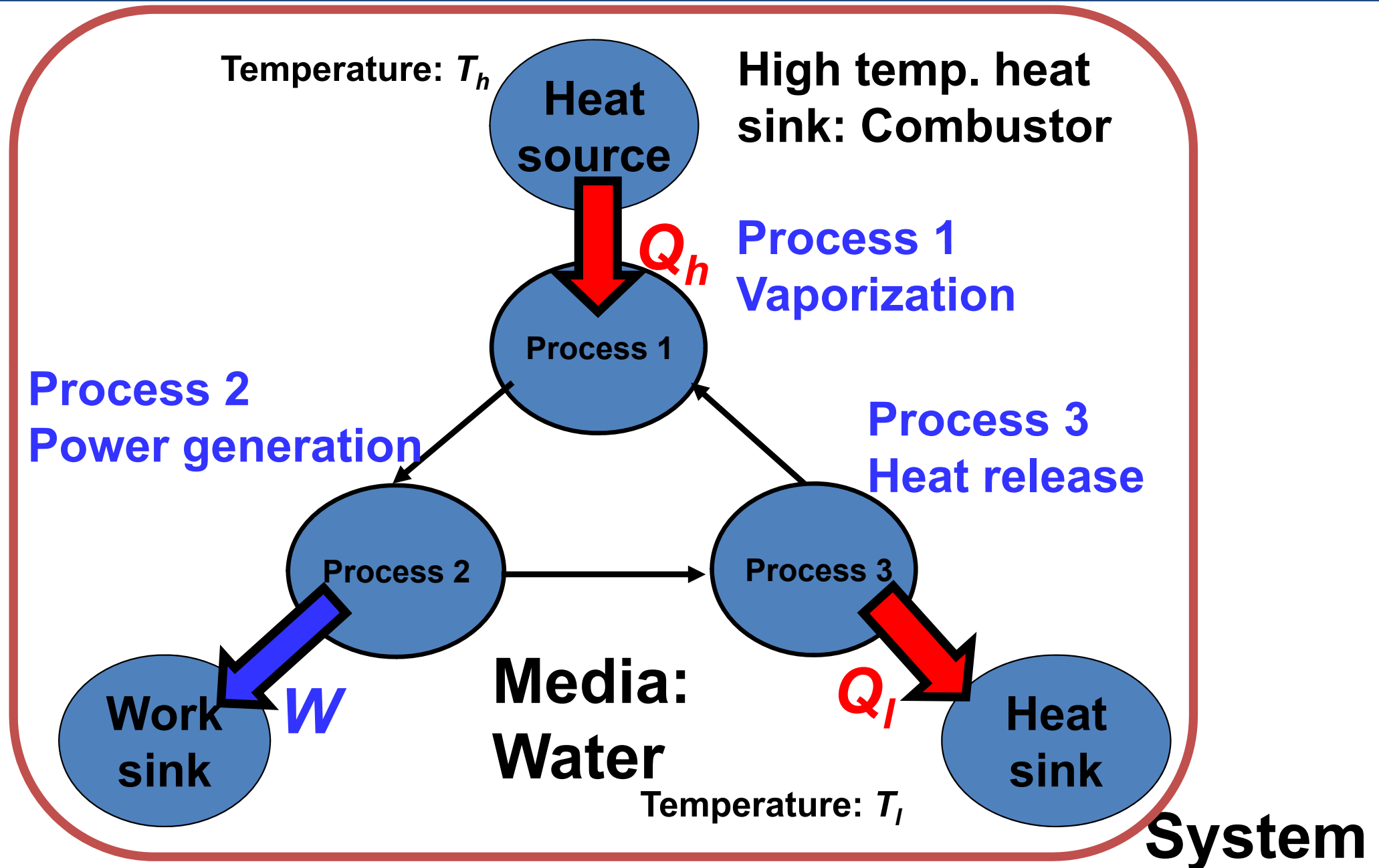
$$W \geq \frac{T_h - T_l}{T_h} Q_h = \frac{[(300) - (270)]}{(300)} (1) = 0.1 [\text{kW}]$$

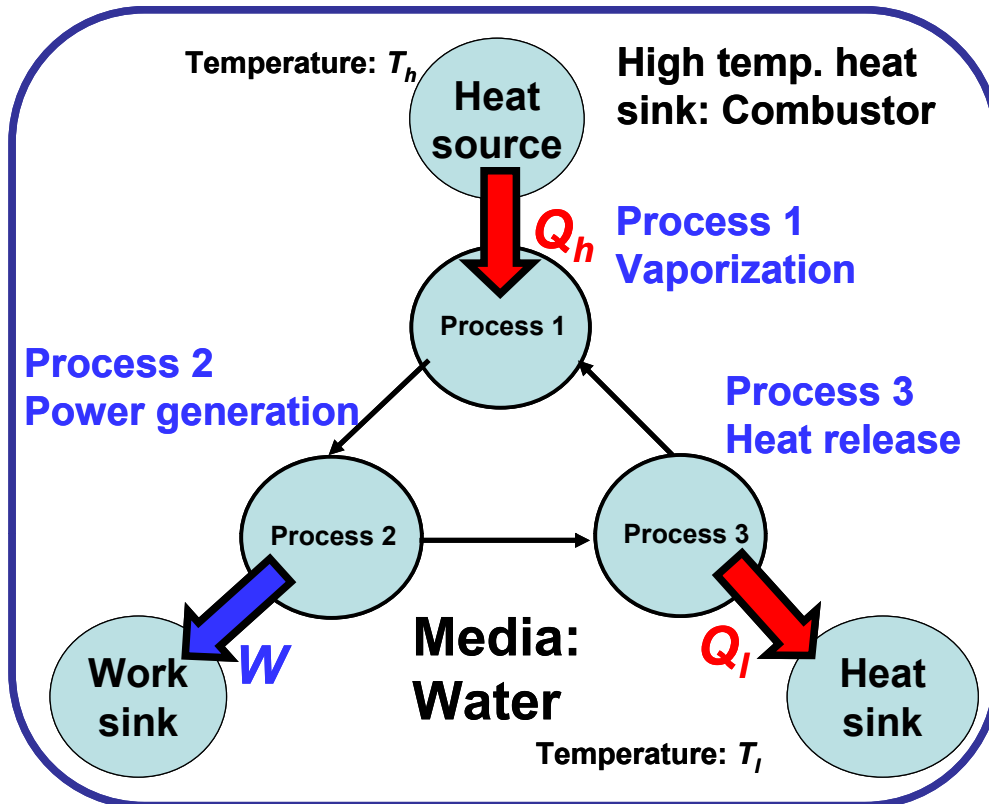
Comparison Joule heating

$$W = 1\text{ kW}$$



Ex.3 Thermodynamic analysis of power generation





$$W - Q_h + Q_l = 0$$

$$-\frac{Q_h}{T_h} + \frac{Q_l}{T_l} \geq 0$$

$$W \leq \frac{T_h - T_l}{T_h} Q_h$$

High temp. heat source: 600°C (=873K)

Low temp. heat sink: 50°C (=323K)

$$W \leq \frac{T_h - T_l}{T_h} Q_h = \frac{[(873) - (323)]}{(873)} Q_h = 0.63 Q_h$$

Temp. of heat source



Conversion efficiency to electricity



$$W - Q_h + Q_l = 0 \quad \longrightarrow \quad Q_l = Q_h - W \geq \frac{T_l}{T_h} Q_h$$

$$-\frac{Q_h}{T_h} + \frac{Q_l}{T_l} \geq 0$$

Heat from high temp. heat source: Q_h

IV

Converted electric energy: W

$$W \leq \frac{T_h - T_l}{T_h} Q_h \quad \longrightarrow \quad \frac{W}{Q_h} \leq \frac{T_h - T_l}{T_h}$$

II

Carnot efficiency  Ratio of the max. work energy taken to thermal energy taken to

Change of Gibbs free energy

$$\Delta G = \Delta H - T \Delta S$$

Temperature: T \longrightarrow Ambient temp. $T_0 (=298\text{K})$

$$\Delta \varepsilon = \Delta H - T_0 \Delta S$$

$\Delta \varepsilon$: Change of exergy [J], [J/s]

The 2nd law $\sum_j \Delta S_j \geq 0$

$$\sum_j \Delta \varepsilon_j = \sum_j \left(\Delta H_j - T_0 \Delta S_j \right) = -T_0 \sum_j \Delta S_j \leq 0$$

Decreasing law of exergy



Quality of energy

Degree of low level d $d = \frac{\Delta S}{\Delta H}$ [1/K]

$\frac{\Delta \varepsilon}{\Delta H} \equiv A$ **Energy level**

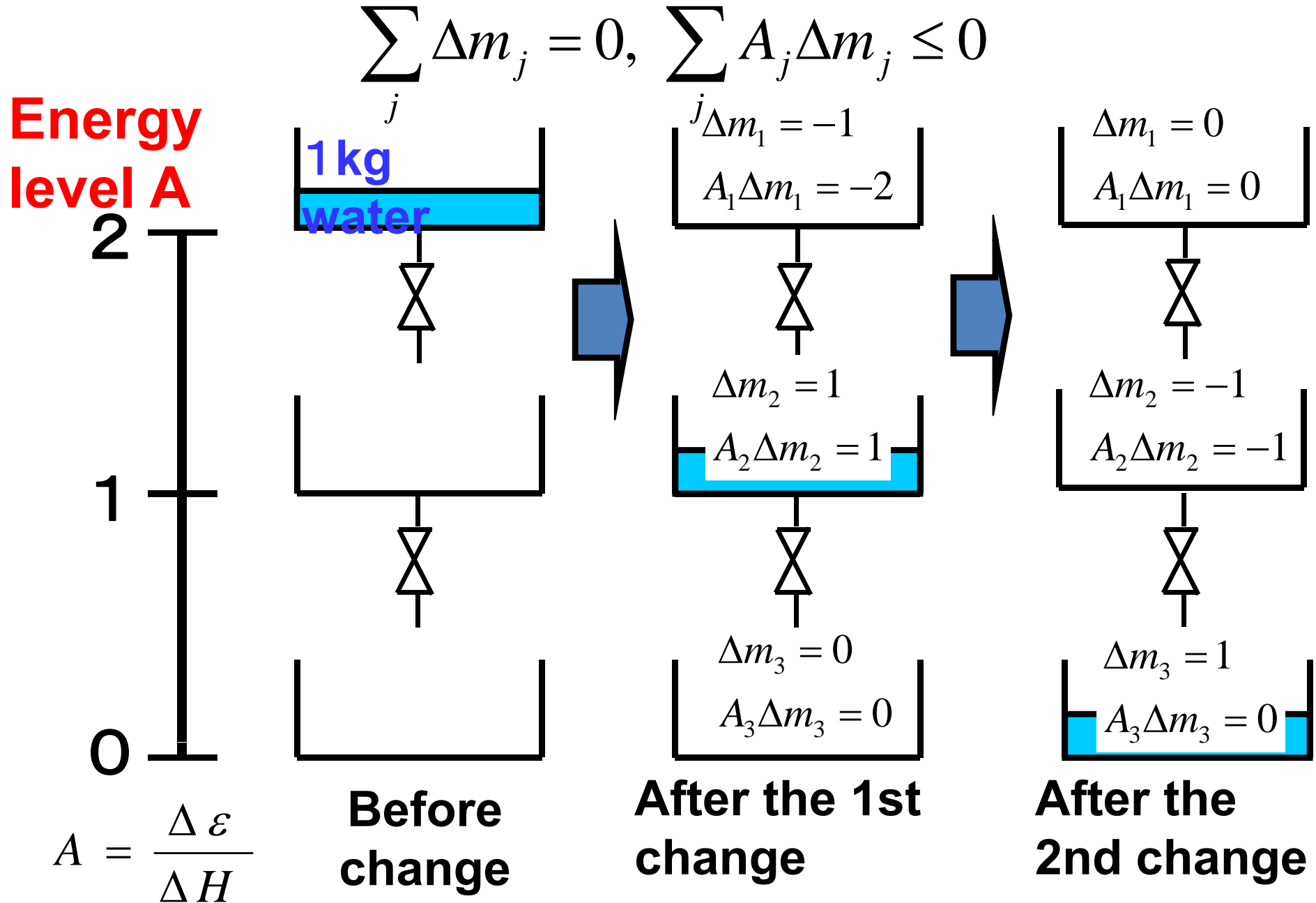
$$A = \frac{\Delta \varepsilon}{\Delta H} = \frac{\Delta H - T_0 \Delta S}{\Delta H} = 1 - T_0 \frac{\Delta S}{\Delta H} = 1 - T_0 d$$

The 1st law $\sum_j \Delta H_j = 0$

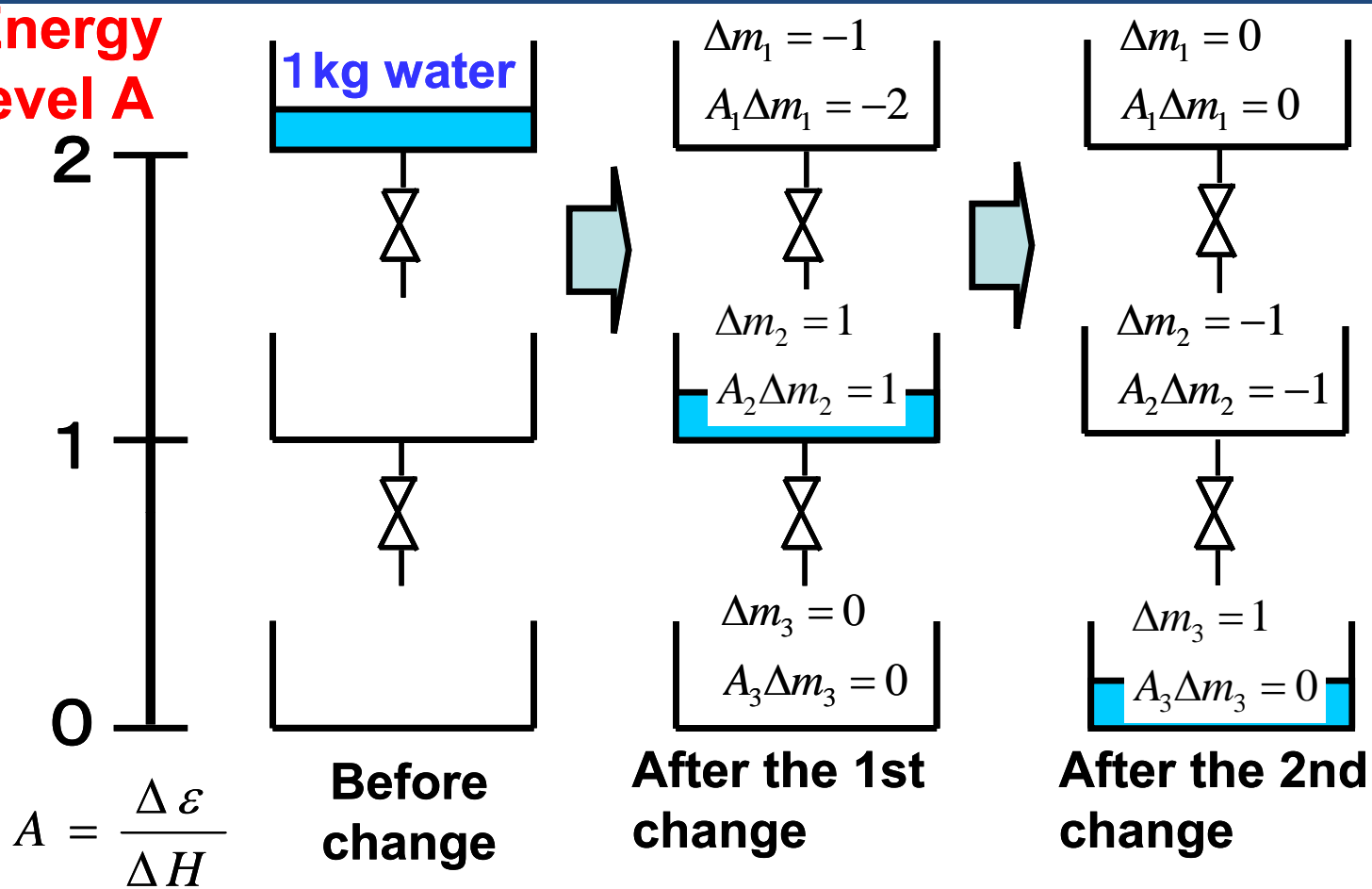
The 2nd law $\sum_j A_j \Delta H_j \leq 0$



Explanation of energy level by Water model



Energy level A



The 2nd law (Decreasing law of exergy)

$$\sum_j \Delta \varepsilon_j = \sum_j A_j \Delta m_j = A_1 \Delta m_1 + A_2 \Delta m_2 + A_3 \Delta m_3 = -1 \leq 0$$

Process	Quantity of energy	Temperature	ΔH	$\otimes \varepsilon$	A
Heat source	Output Q	T	$-Q$	$-\frac{T-T_0}{T}Q$	$\frac{T-T_0}{T}$
Heat sink	Input Q	T	Q	$\frac{T-T_0}{T}Q$	$\frac{T-T_0}{T}$
Work source	Output W	—	$-W$	$-W$	1
Work sink	Input W	—	W	W	1

$$\Delta \varepsilon = \Delta H - T_0 \Delta S$$

$$A = \frac{\Delta \varepsilon}{\Delta H}$$

Energy level of work source and sink = 1

Energy level of heat source and sink \Rightarrow Carnot efficiency at $T_f = T_0$

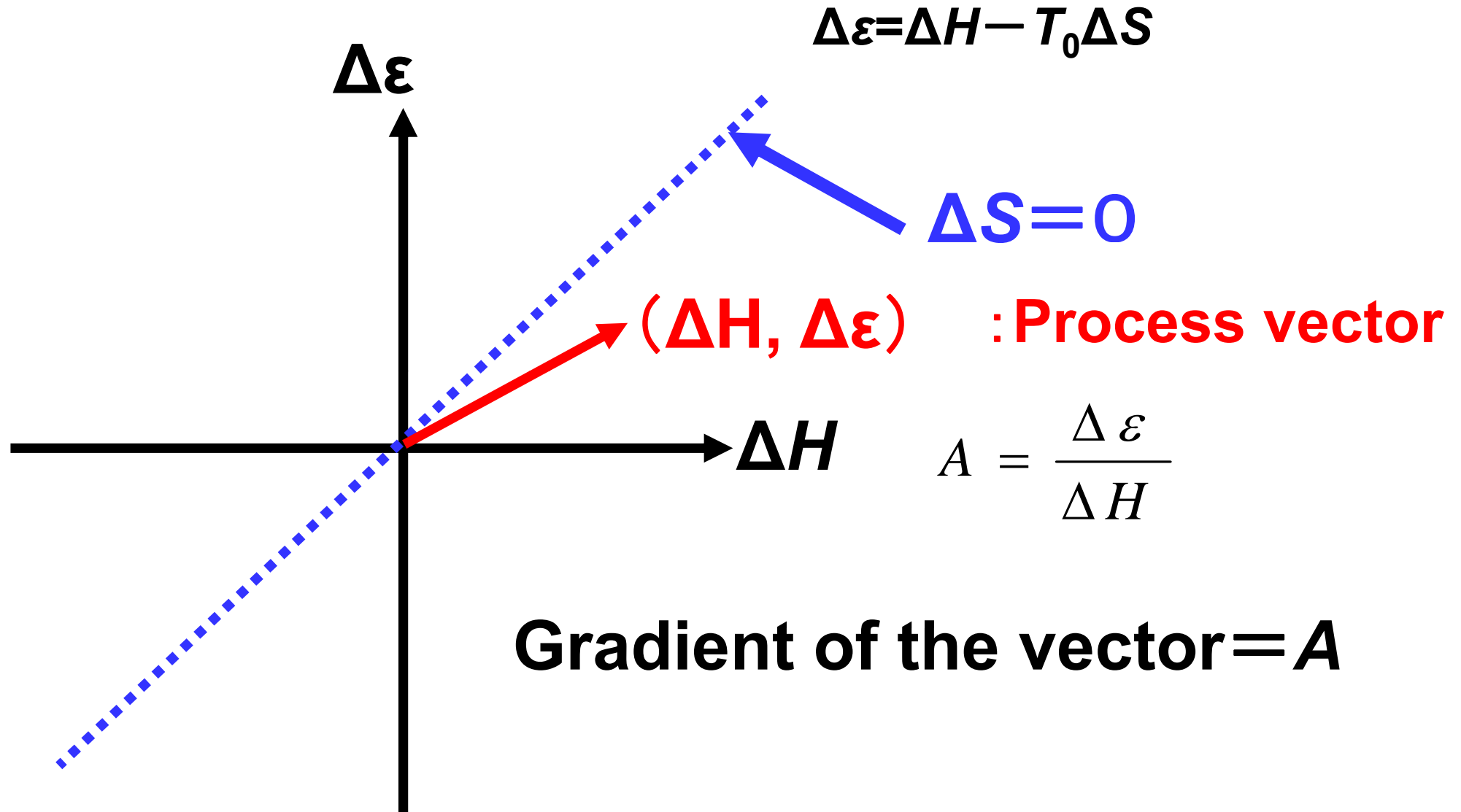
Temp. of heat source and sink = T_0 $A=0$

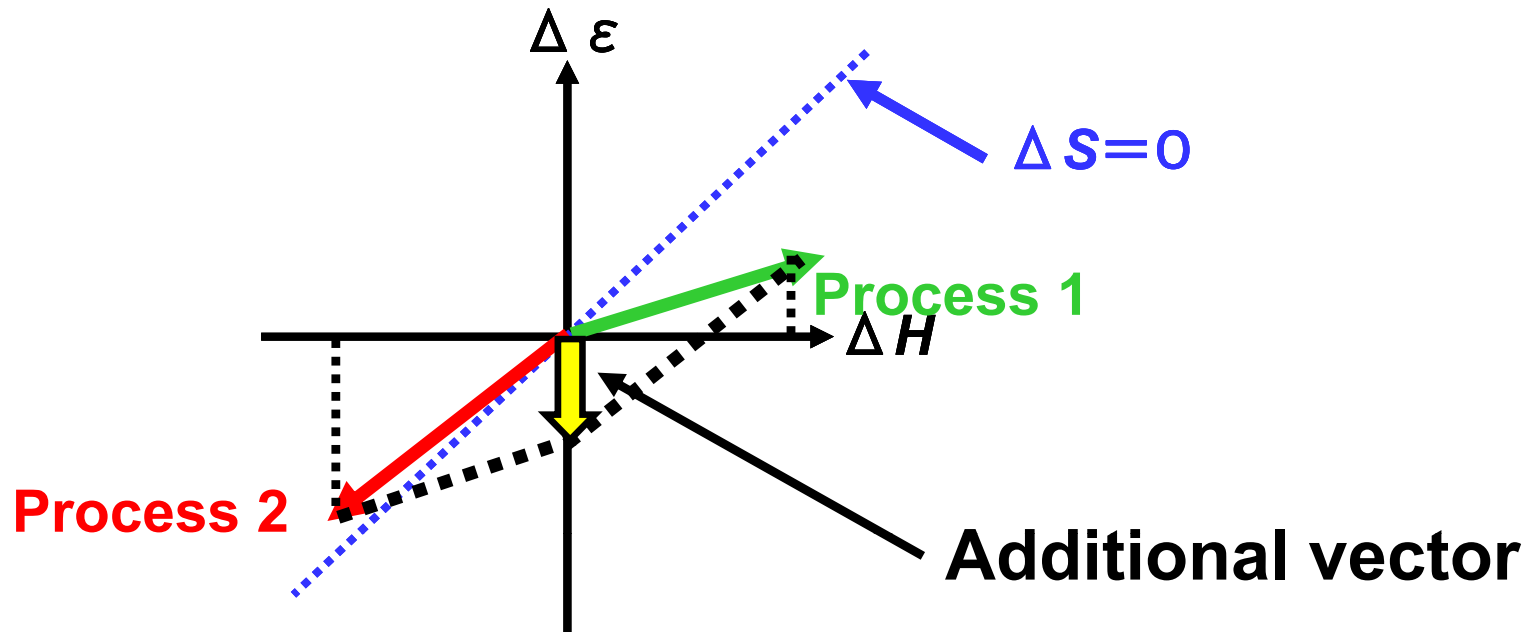
Temp. of heat source and sink = ∞ $A=1$

\leftarrow Corresponding to work source and sink

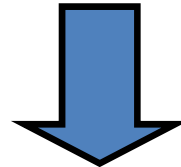


Thermodynamic compass?





Expression of the 1st and 2nd laws on the coordinate
System: Addition of two process vectors



The additional vector must be negative or 0 on the $\Delta\varepsilon$ axis

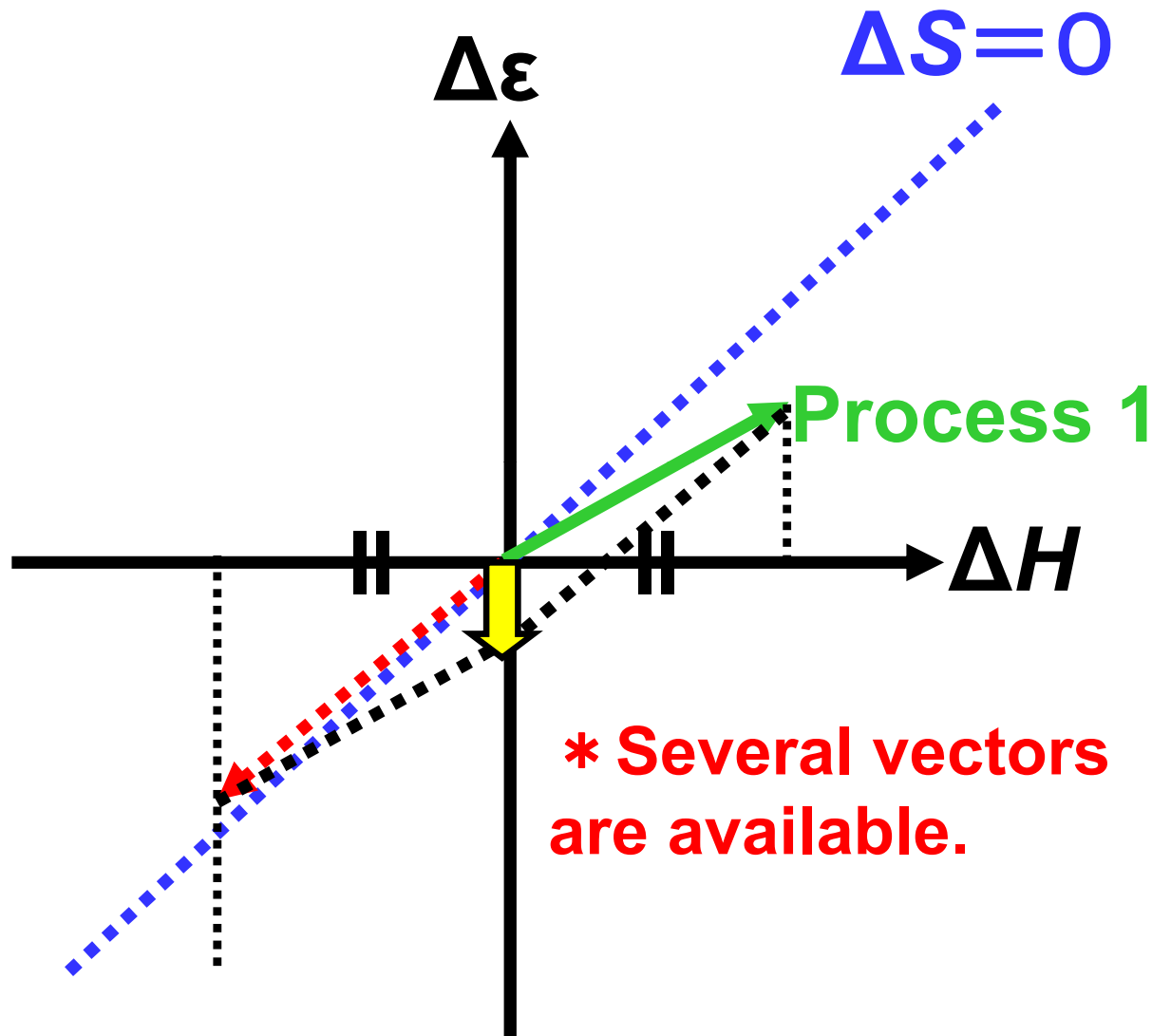
Reasons The 1st law

$$\sum_j \Delta H_j = 0$$

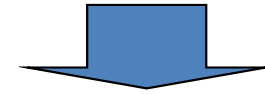
The 2nd law

$$\sum_j \Delta \varepsilon_j \leq 0$$

How to use the thermodynamic vector



Determination of Process 1



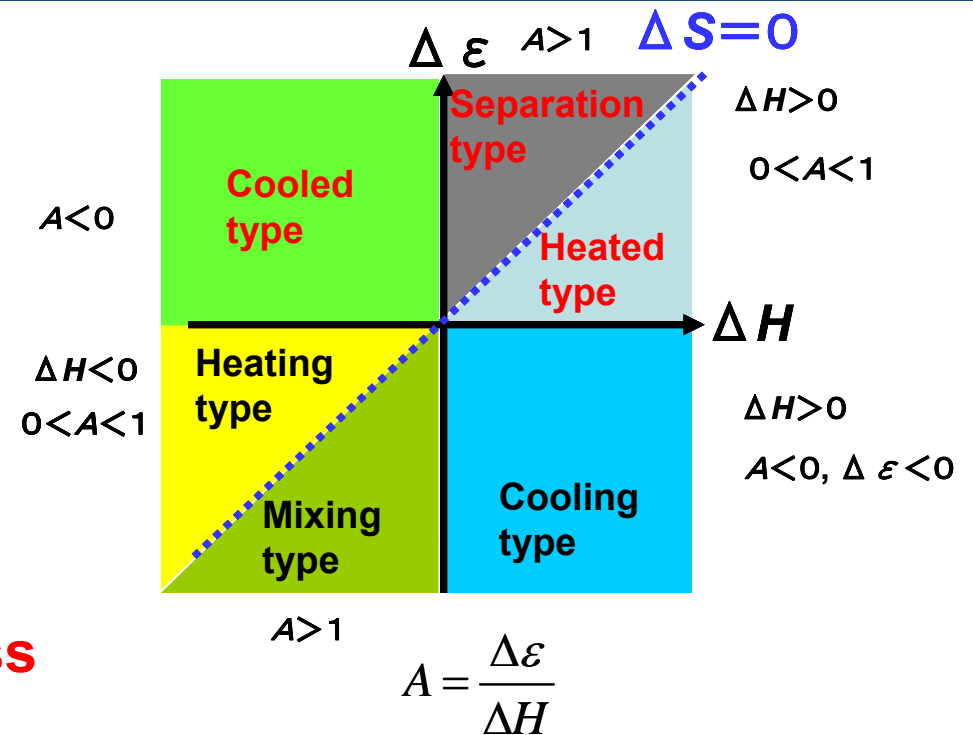
Finding the vector to satisfy that the additional vector must be negative on the $\Delta \varepsilon$ axis

The 1st law

$$\sum_j \Delta H_j = 0$$

The 2nd law

$$\sum_j \Delta \varepsilon_j \leq 0$$



Red processes: Depending on process

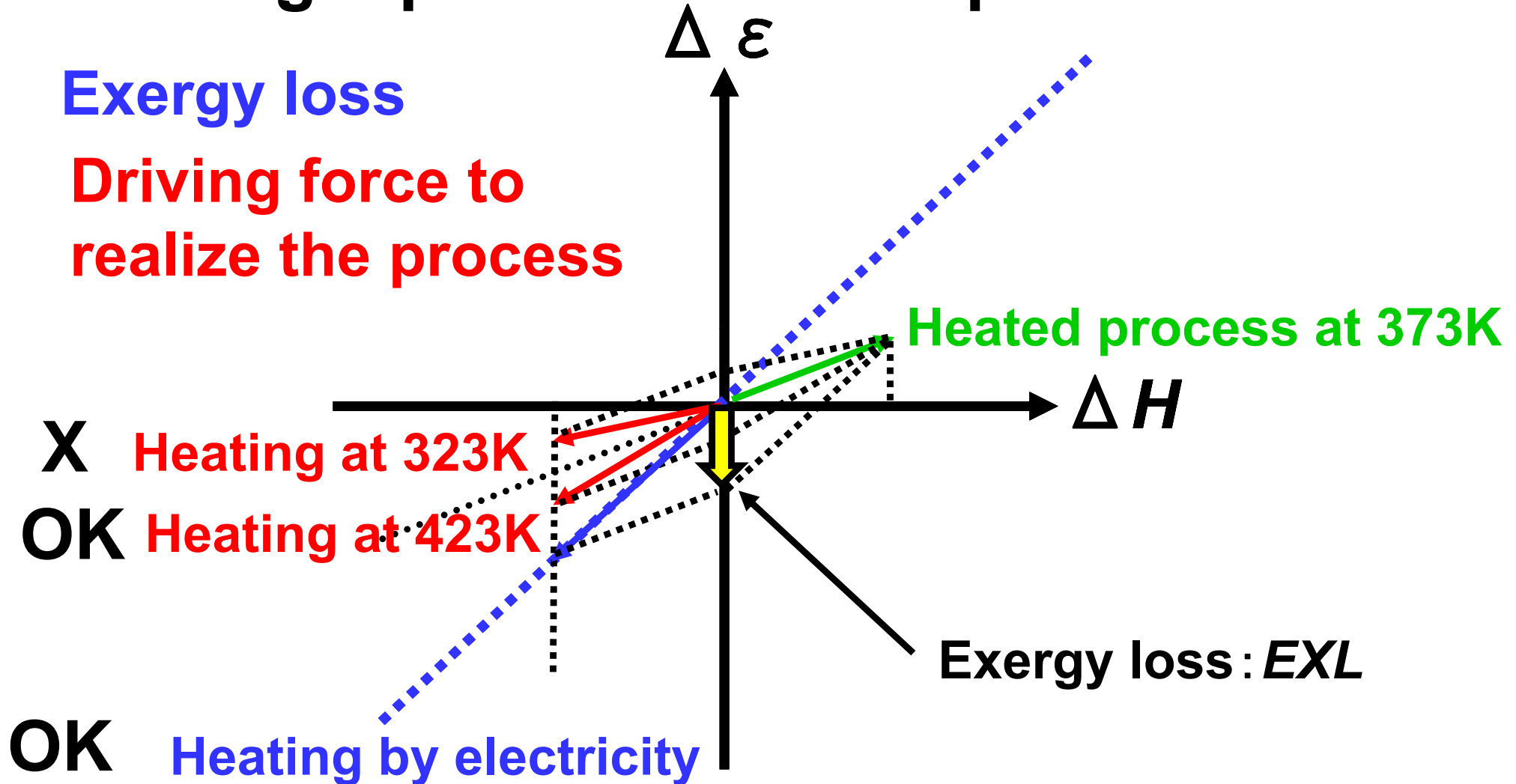
Process examples

- Heated type** Temp. increase from 100°C to 200°C
- Heating type Temp. decrease from 200°C to 100°C
- Cooling type Temp. increase from -50°C to -30°C
- Cooled type** Temp. decrease from -30°C to -50°C
- Separation type** Separation of air to N₂ and O₂
- Mixing type Mixing of N₂ with O₂



Process selection against target process

Ex. Target process: Heated process at 373K



Max. exergy loss: Utilization of electricity



$$A = \frac{T - T_0}{T}$$

$$T_0 = 298 \text{ [K]}$$

$$A = 0.5$$

$$T = \frac{T_0}{A - 1} = \frac{298}{(0.5) - 1} = 596 \text{ [K]}$$

Thermal energy $-\infty < A \leq 1$

$\Delta \varepsilon$

Cooled type

$A = -0.5$
 $T = 199 \text{ K}$

$A = 1$
 $T = \infty$

Work sink

$A = 0.5$
 $T = 596 \text{ K}$ **Heated type**

ΔH

Heating type

$A = 0.5$
 $T = 596 \text{ K}$

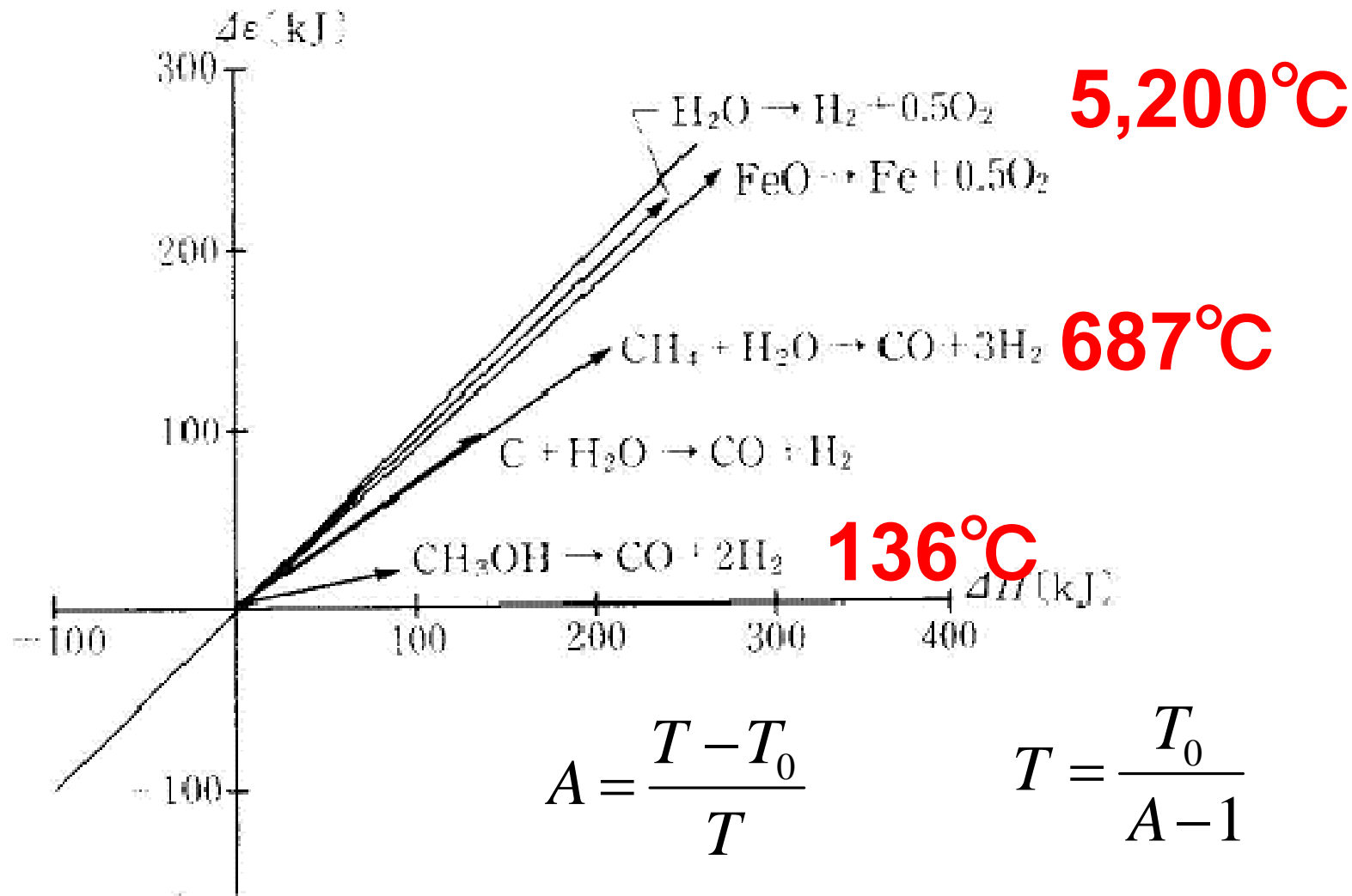
$A = 0$
 $T = 298 \text{ K}$

$A = -0.5$
 $T = 199 \text{ K}$ **Cooling type**

Work source $A = 1$
 $T = \infty$



Example of vectors of endothermic reaction



Example of vectors of exothermic reaction

